

# Density Matrix Renormalization Group Studies of Correlated Quantum States Emerging in Moire Materials and Beyond

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U.S. DEPARTMENT OF  
**ENERGY**

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Science

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# Collaborations

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Z. Zhu. et al., [arXiv1812.05661](https://arxiv.org/abs/1812.05661) and to be submitted

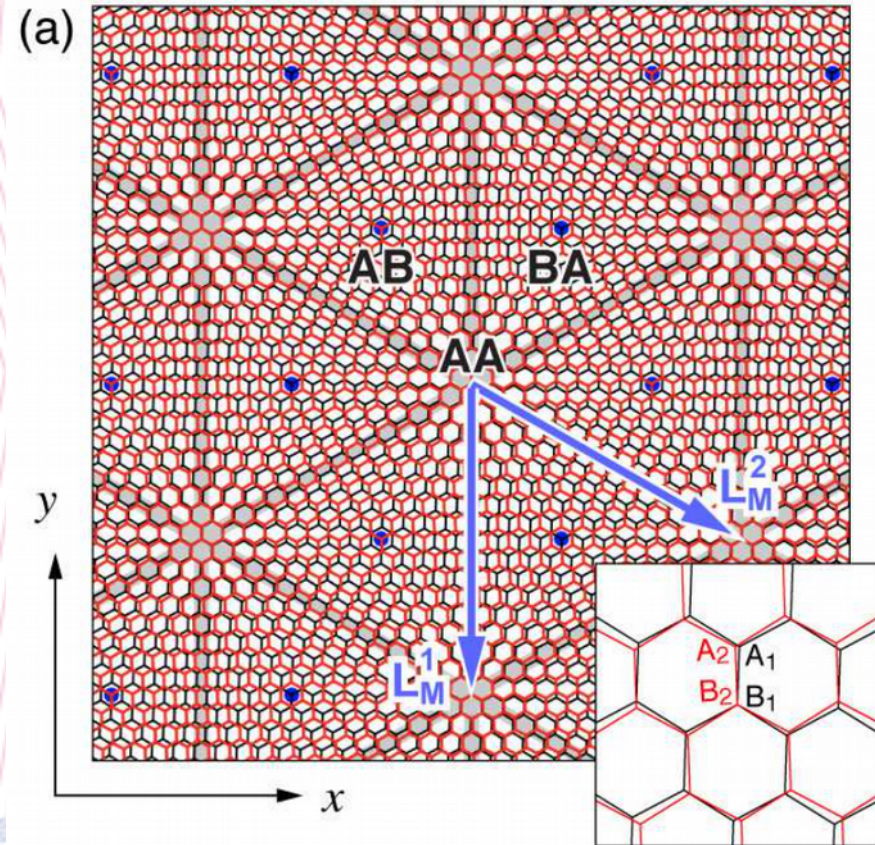
# Outline

## DMRG Studies of Two-Component Hubbard Models for Moire Materials

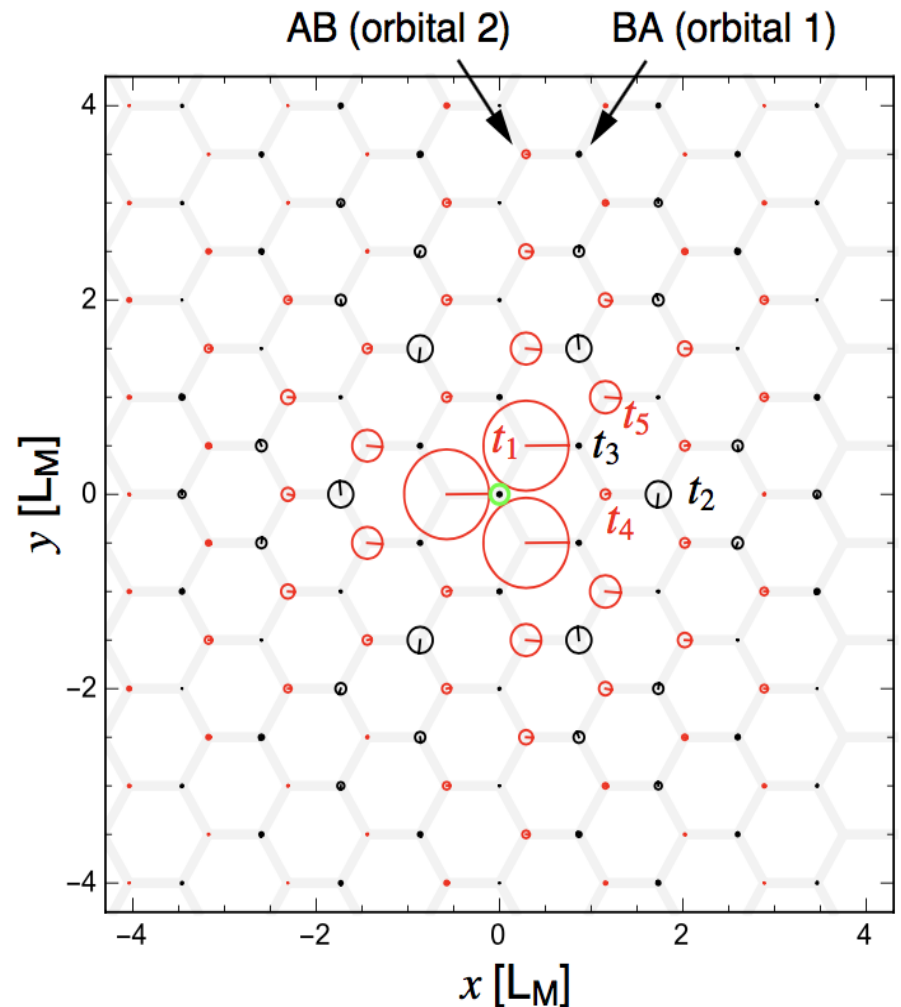
- Twisted bilayer graphene
- Trilayer graphene-boron nitride with Moire potential

**Spin Liquid in Spin-One Kitaev Material**

# SU4 Hubbard model for twisted graphene

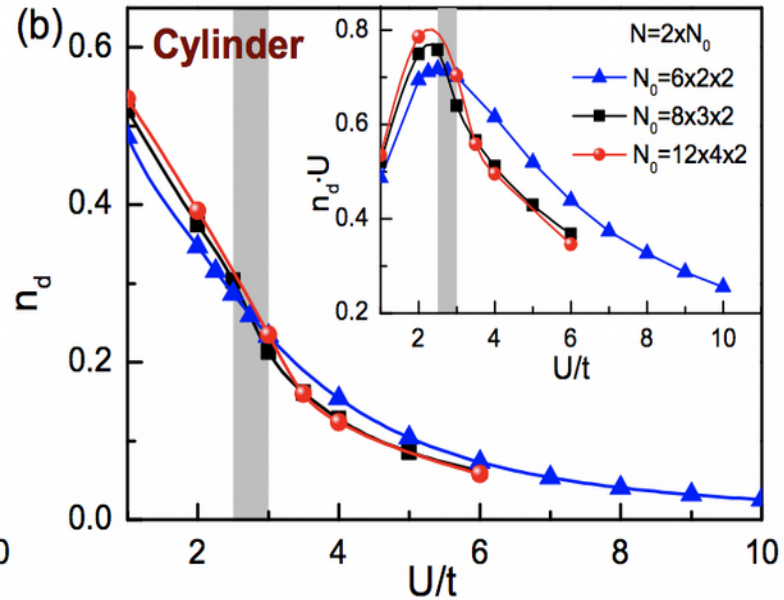
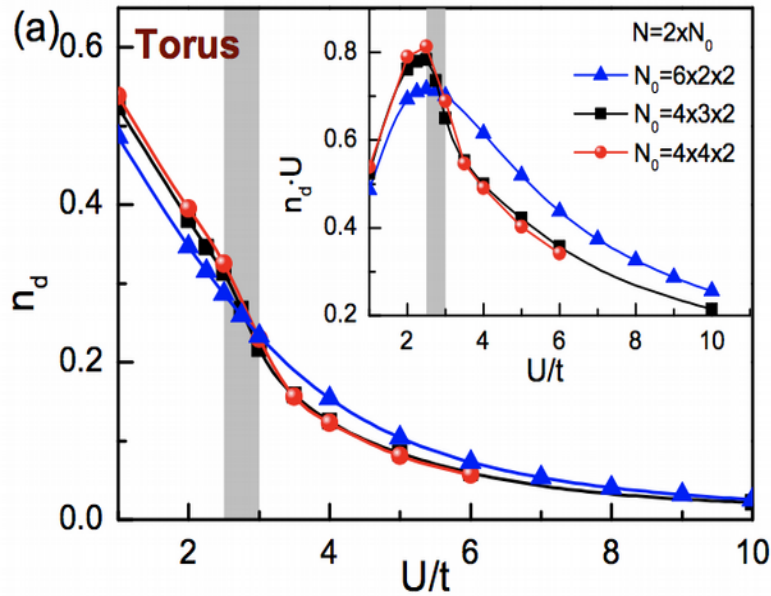


(a) From orbital 1



Koshino et al.(18)

# Hubbard U driven transition



$$H = H_0 + H_{\text{int}},$$

$$H_0 = -t \sum_{\langle i,j \rangle} \sum_{\sigma} \sum_{\alpha=1,2} \left( c_{i\sigma,\alpha}^\dagger c_{j\sigma,\alpha} + h.c. \right),$$

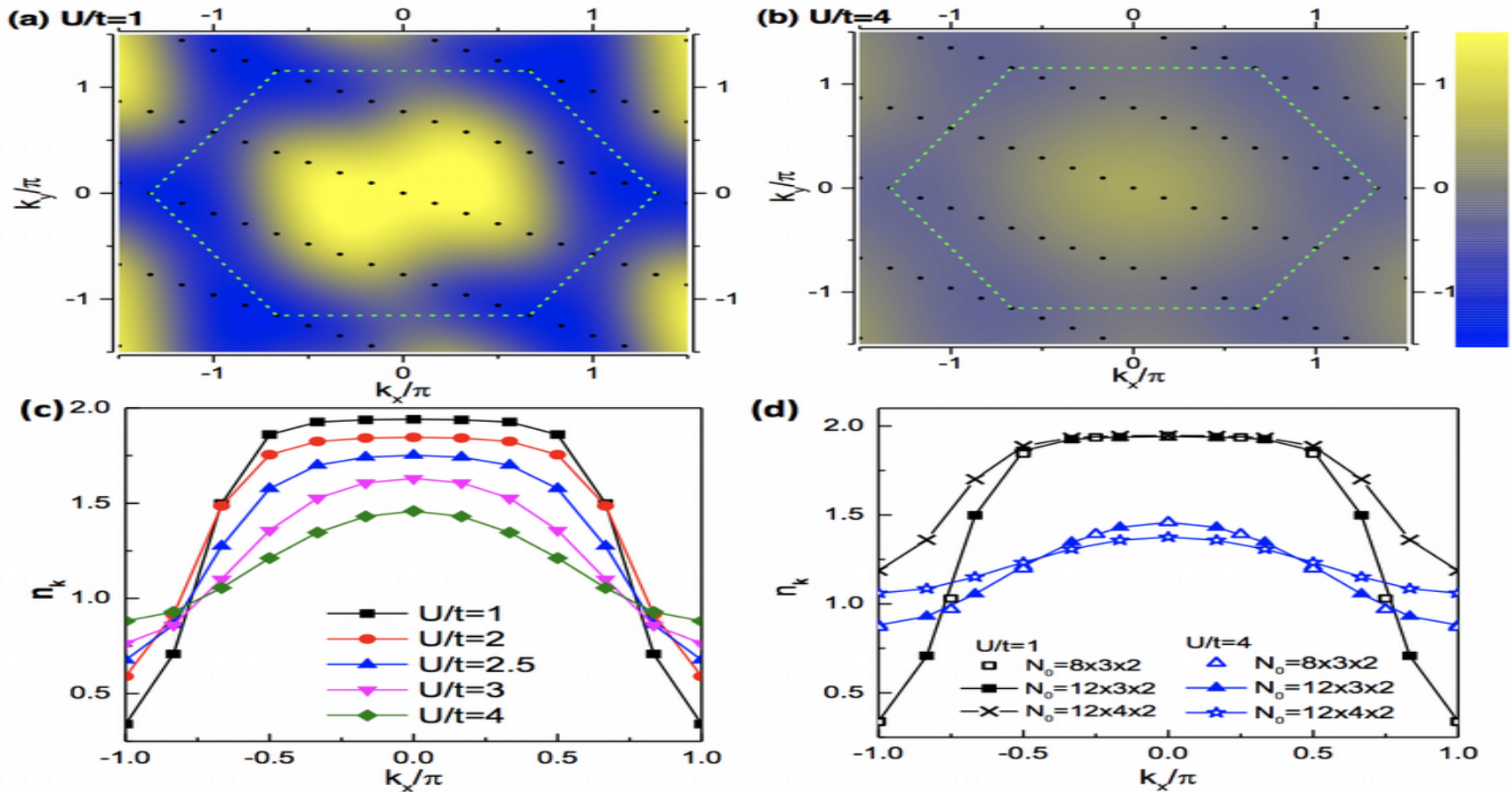
$$H_{\text{int}} = U \sum_i \left( \sum_{\sigma,\alpha} n_{i\sigma,\alpha} - 1 \right)^2,$$

Identifying  $U_c \sim 3$

We consider  $1/4$  filling number  
That is one electron per  
unit cell

$$n_d = \frac{1}{N_0} \sum_{i=1}^{N_0} \left\langle \left[ \sum_{\sigma,\alpha} n_{i\sigma,\alpha} - 1 \right]^2 \right\rangle,$$

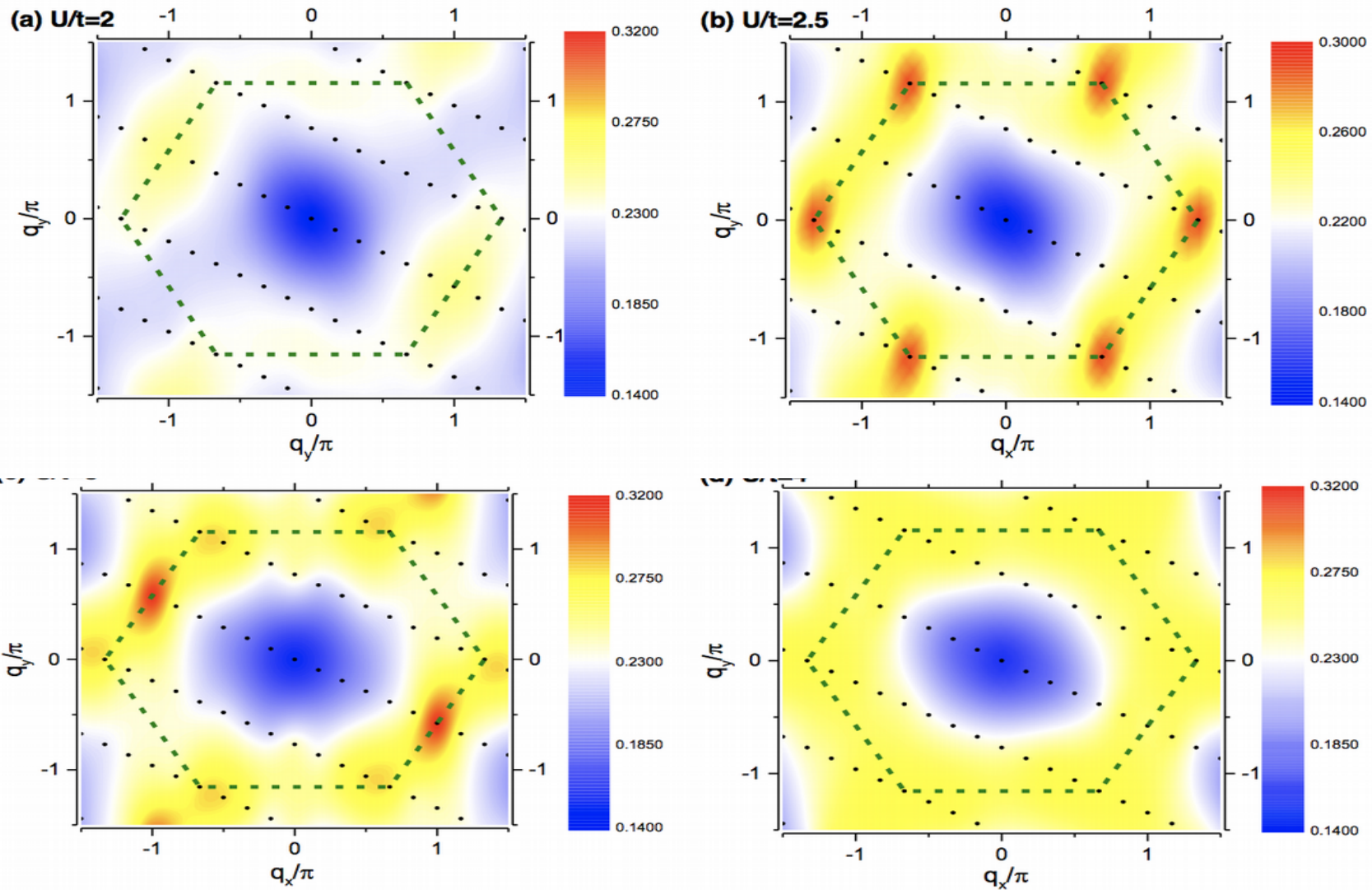
# Fermi-surface topology



$$n(\mathbf{k}) = \frac{1}{N_0} \sum_{i,j,\sigma} \langle c_{i\sigma}^\dagger c_{j\sigma} \rangle e^{i\mathbf{k}(\mathbf{r}_i - \mathbf{r}_j)}.$$

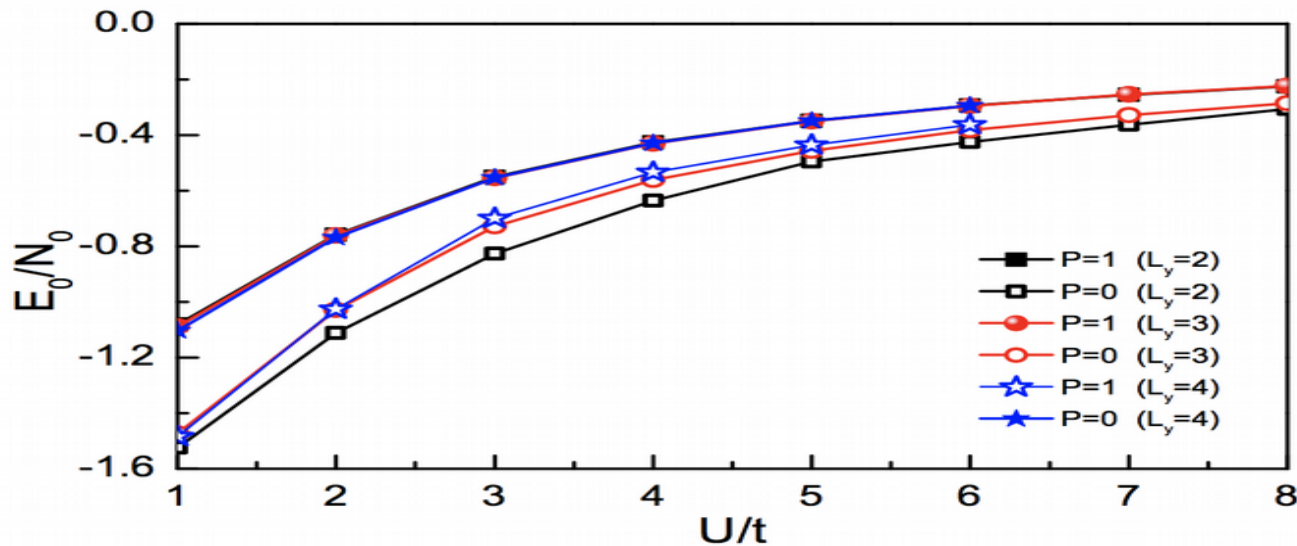
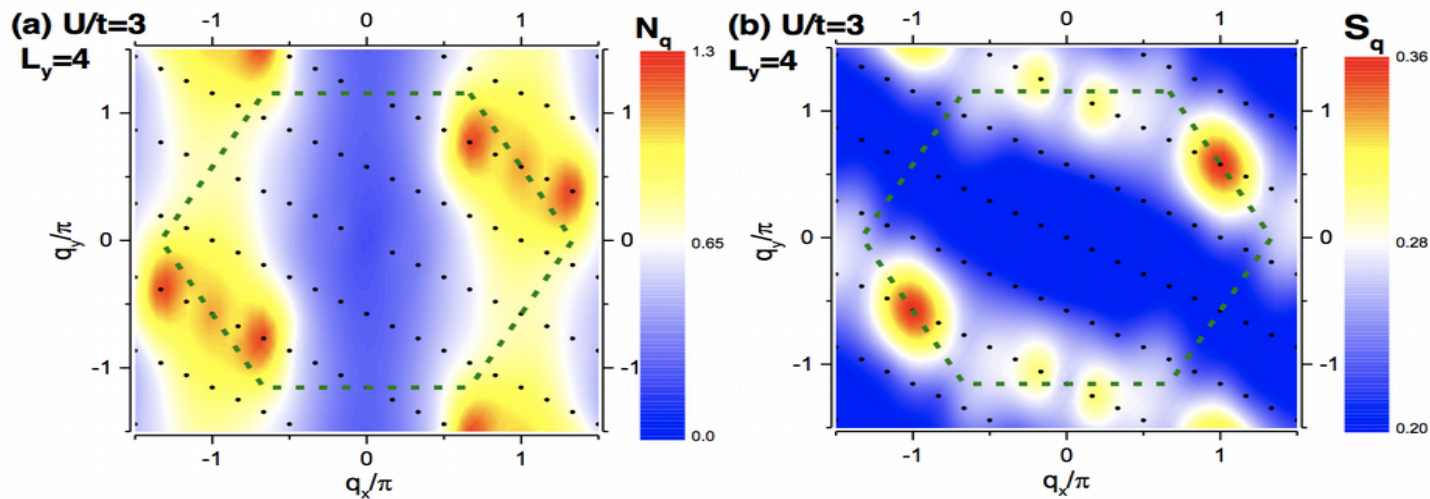
Mott insulator  
At  $U > U_c$

# Spin/orbital density structure factor



$$S_{\mathbf{q}} = \frac{1}{N_0} \sum_{i,j} \langle S_i^z S_j^z \rangle e^{i\mathbf{q}(\mathbf{r}_i - \mathbf{r}_j)}.$$

# Robust spin/orbital peak at larger $L_y=4$

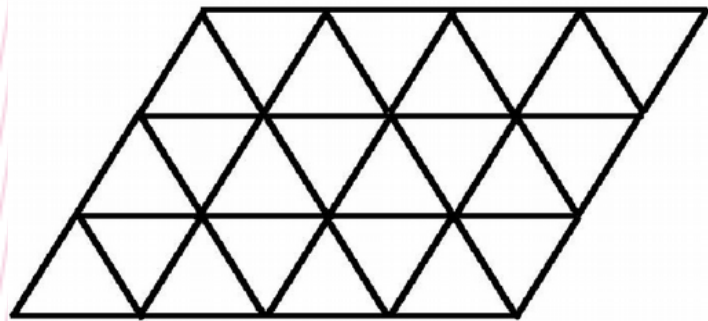


No valley polarization

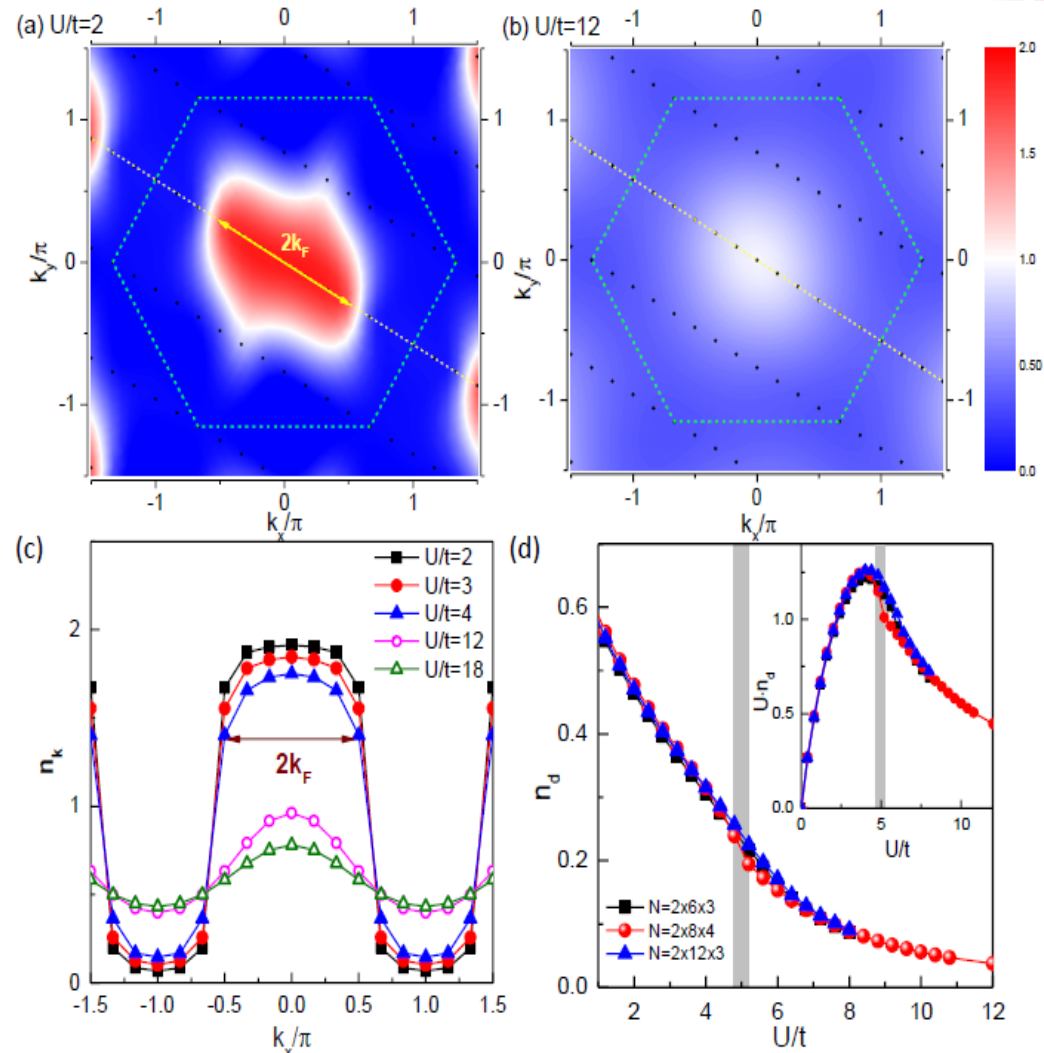


# SU4 Hubbard Model for Trilayer Graphene-Boron Nitride and Twisted Transition Metal Dichalcogenides

$$H = -t \sum_{\langle i,j \rangle, \sigma\alpha} (c_{i,\sigma\alpha}^\dagger c_{j,\sigma\alpha} + h.c.) + U \sum_i (\sum_{\sigma\alpha} n_{i,\sigma\alpha} - 1)^2$$

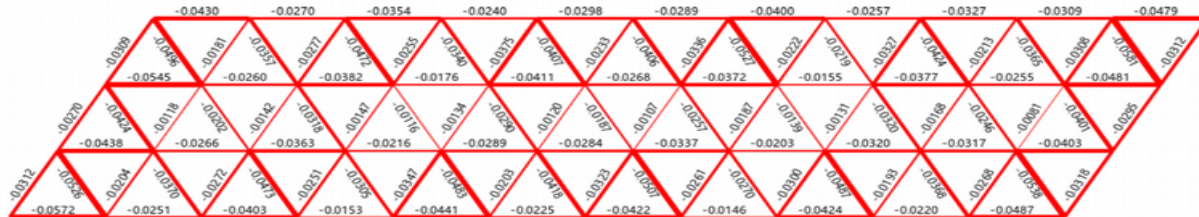


We consider  $\frac{1}{4}$  filling number, one electron per unit cell



# Stripe VBS appears with larger U

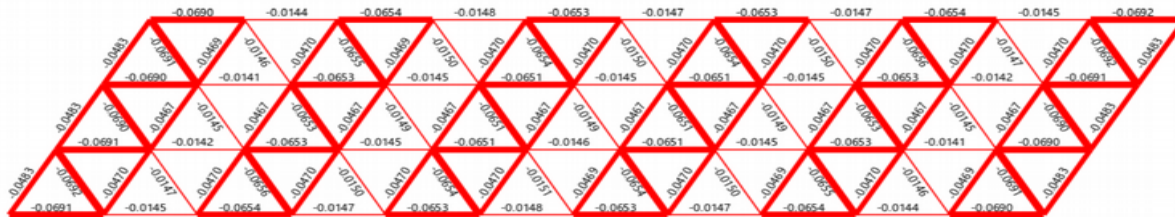
(a)  $N=2 \times 12 \times 4$   $U/t=3$



(b)  $N=2 \times 12 \times 4$   $U/t=6$

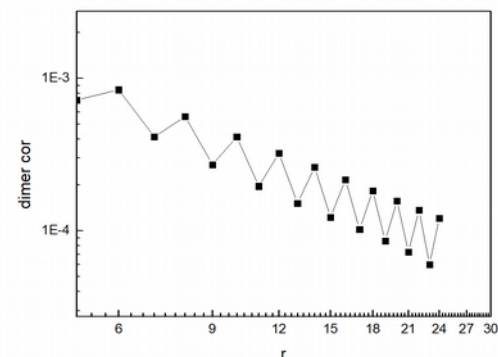
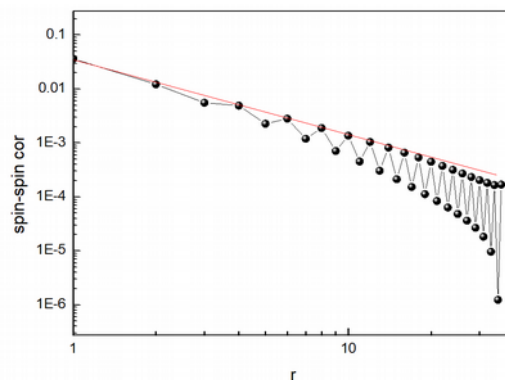
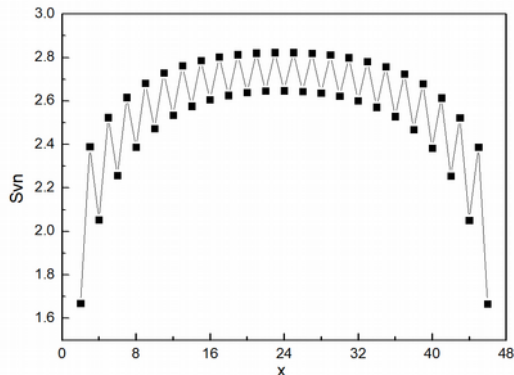


(c)  $N=2 \times 12 \times 4$   $U/t=12$



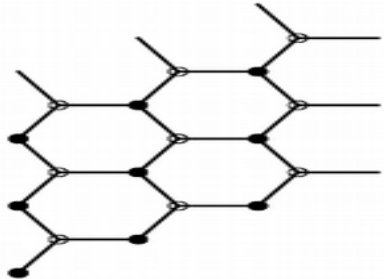
with possible  
gapless  
excitations due  
to half filling of  
each unit cell

Finite central  
charge from  
entanglement  
entropy



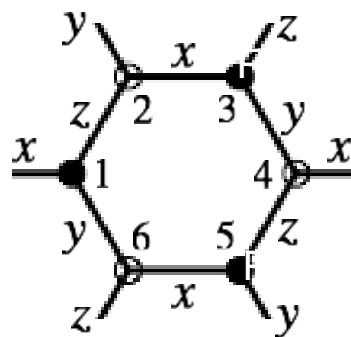
# Spin-1 Kitaev-Heisenberg model

$$\hat{H} = K_x \sum_{\langle i, i \rangle} S_i^x S_j^x + K_y \sum_{\langle i, j \rangle_y} S_i^y S_j^y + K_z \sum_{\langle i, j \rangle_z} S_i^z S_j^z + J \sum_{\langle i, j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$



$$W_L = e^{i\pi S_1^{\alpha_{12}}} e^{i\pi S_2^{\alpha_{12}}} e^{i\pi S_2^{\alpha_{23}}} e^{i\pi S_3^{\alpha_{23}}} \dots e^{i\pi S_{(n-1)}^{\alpha_{(n-1)n}}} e^{i\pi S_n^{\alpha_{(n-1)n}}} e^{i\pi S_n^{\alpha_{n1}}} e^{i\pi S_1^{\alpha_{n1}}}$$

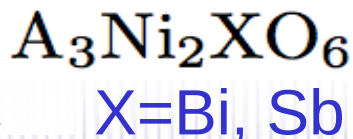
$$W_p = e^{i\pi S_1^z} e^{i\pi S_2^z} e^{i\pi S_2^x} e^{i\pi S_3^x} e^{i\pi S_3^y} e^{i\pi S_4^y} e^{i\pi S_4^z} e^{i\pi S_5^z} e^{i\pi S_5^x} e^{i\pi S_6^x} e^{i\pi S_6^y} e^{i\pi S_1^y}$$



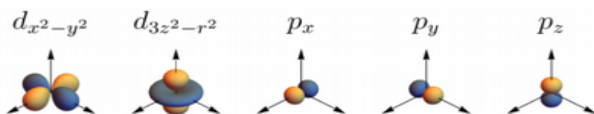
$$W_p = \sigma_1^x \sigma_2^y \sigma_3^z \sigma_4^x \sigma_5^y \sigma_6^z$$

$$W_p = e^{i\pi S_1^x} e^{i\pi S_2^y} e^{i\pi S_3^z} e^{i\pi S_4^x} e^{i\pi S_5^y} e^{i\pi S_6^z}$$

Stavropoulos et al



Conserved Wilson loop operators



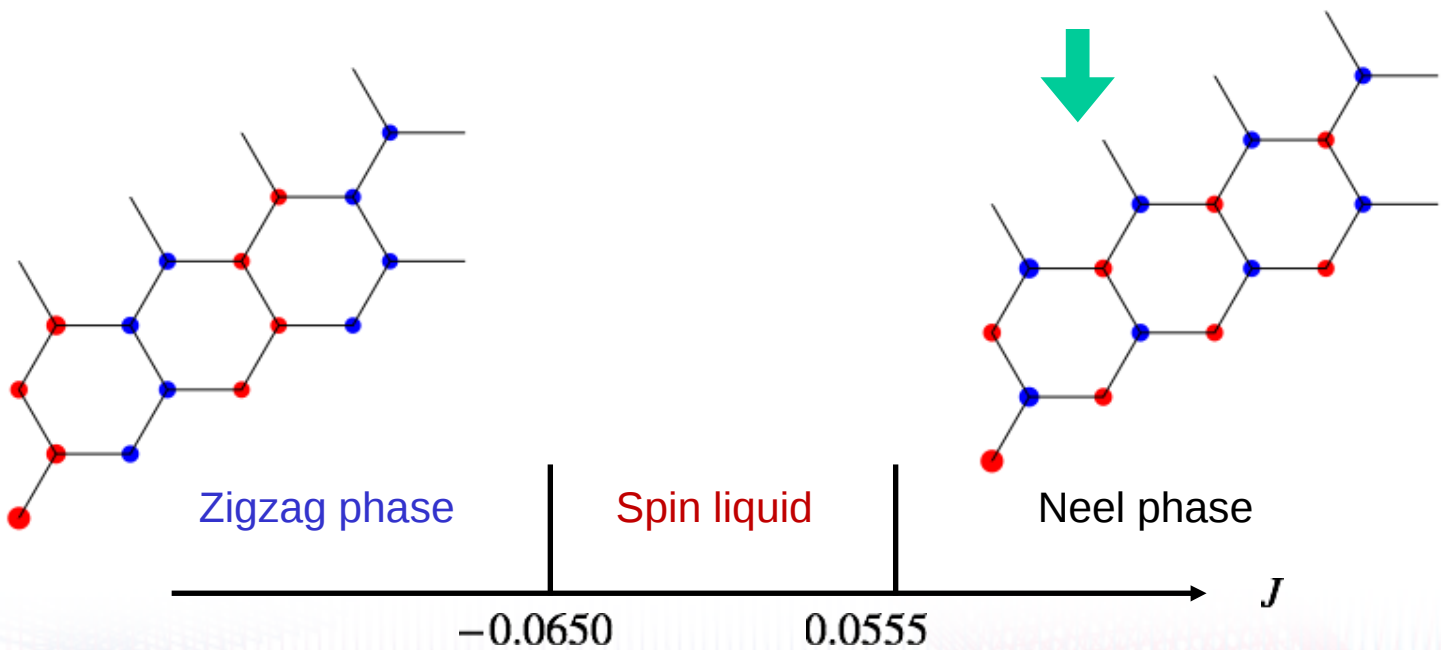
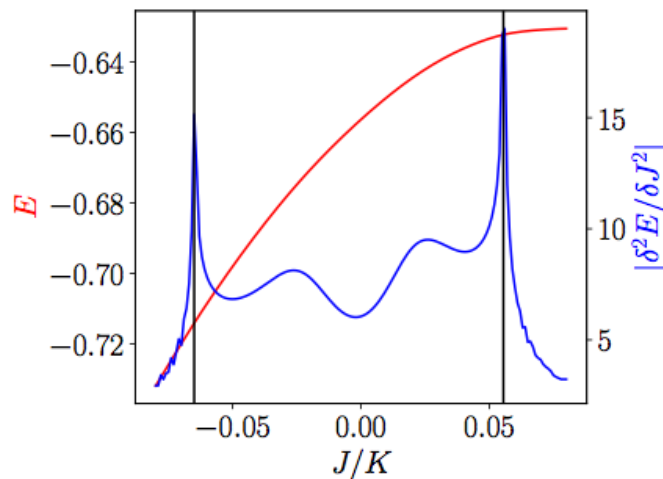
# Phase diagram

$$\hat{H} = K_x \sum_{\langle i,j \rangle_x} S_i^x S_j^x + K_y \sum_{\langle i,j \rangle_y} S_i^y S_j^y + K_z \sum_{\langle i,j \rangle_z} S_i^z S_j^z + J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$

$$K = 1.0$$

$$L_y = 2$$

iDMRG



# Summary

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Large scale DMRG studies reveal different possible correlated phases for multi-orbital Hubbard models.

These results may be relevant for understanding twisted and trilayer graphene subject to Moire patterns.

Interesting gapless spin liquid is also found for  $S=1$  Kitaev model