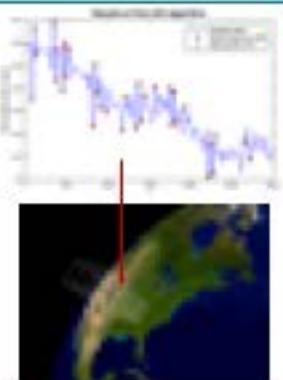


FASTMath Team Members: R. Archibald¹, F. Bao³, A. Gelb², H. Tran¹, & C. Webster^{1&4}

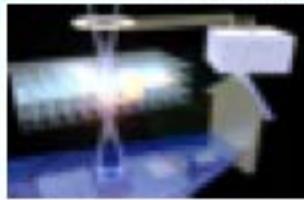
Sparse functional representation of data, to enable faster IO and analysis of big datasets

In-situ analysis of streaming climate data

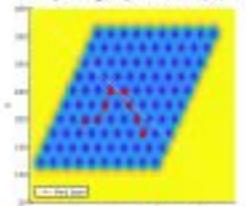
- Developing effective online data monitoring and archiving strategy over temporal and spatial domains while respecting practical storage and memory capacity constraints
- Streaming methods improves the quality and quantity of information available to scientists for analysis



Atomic Force Analysis



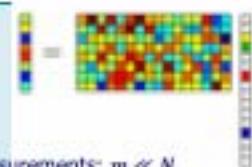
Left: Tracking of multiple well potential in 1D.



Right: Tracking of multiple well lattice potential in 2D.

Sparse data representations

- We reconstruct data $c \in \mathbb{R}^{N \times 1}$ from measurements $u \in \mathbb{R}^{m \times 1}$ and $A \in \mathbb{R}^{m \times N}$.
- $u \approx Ac$
- Limited number of measurements: $m \ll N$.
- The data are sparse.
- $l = 1$: reconstructing a single dataset.
- $l > 1$: simultaneously reconstructing multiple datasets.
- Recovery via regularizations enforcing sparsity:
 $c = \operatorname{argmin}_z R(z) \text{ subject to } u \approx Az$

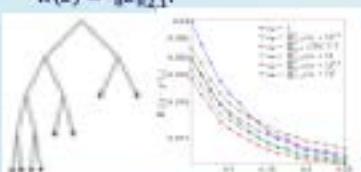


Standard CS: $R(z) = \|z\|_1$.

Structures of the sparsity can be exploited:

- Downward closed and tree structures:
 $R(z) = \|z\|_{w,1}$.

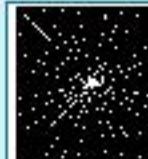
- Joint sparsity:
 $R(z) = \|z\|_{2,1}$.



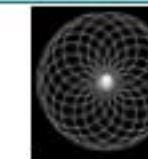
A comparison of adaptive weighted ℓ_1 minimization with different choices of weights

$$R(z) = \|z\|_{w,1} \text{ with } w_j = \max |A_{j,:}|$$

Sampling and fast algorithms



Tomography



MR



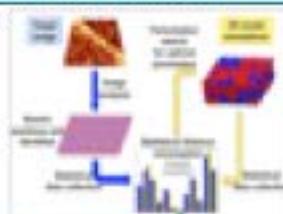
Ultrasound



Thin plate projections of additive manufactured compound

Knowledge Extraction from Images

- Atomic resolution imaging data is readily abundant given advances in instrumentation
- No framework to extract knowledge from data
- We utilize concept of statistical distance to derive materials properties from atomic resolved data, providing a generative model exists



- Acquisition of current-voltage curves for electronic materials characterization at the nanoscale dates back decades
- We increase speed of acquisition by 1000x through full information capture + Bayesian inference methods