

II. Introduction to Tokamak (a 3D Torus)

Torus, not a straight cylinder: plasma is on inhomogeneous physical space (magnetic field) → complicates physics (& math) through magnetic mirroring, curvature drift, ballooning, toroidal mode coupling, etc.

What Science Are We Studying?

- Edge plasma self-organizes into a steep pedestal shape (H-mode) → Smaller & cheaper tokamak, by allowing a hot plasma at plasma edge
- Edge plasma physics is a challenging issue: Plasma contacts material wall. Particle orbits and turbulence are across magnetic separatrix. → non-equilibrium thermodynamics and non-Maxwellian → Outside of a fluid theory regime

An approach to solve PDE on a 5D-grid has been difficult. Particle-in-cell approach → Extreme scale computing is necessary

Critical Edge Physics to Help ITER

- How does the pedestal grow?
- How does the core pressure grow together with edge pressure?
- What determines pedestal shape?
- How localized the heat load will be on divertor plate?
- How does the plasma fueled into core against gradient?
- Why is there a rotation source at edge and how does it propagate in?
- How are edge localized modes (ELMs) triggered and how to suppress them?
- What is the physics for bifurcation from L-mode E, to H-mode E?
- What is the threshold P_{L-2H} ?

The Strategy

- Solve the non-equilibrium problem from first-principles kinetic equation
- Simulate realistic device, including magnetic X-point, sources and sinks
- Avoid neglecting important effects
 - Toroidal mode coupling
 - Coupling of radial drift motions to turbulent field variations
 - Variation of background profile (free energy driver)
 - (Neglect of these effects are called "local" approximation.)
- We choose a scheme stable to the multiscale dynamics
 - Multiscale dynamics: Orbital motions across a large scale fluctuation of the background field could severely violate CFL condition if 5D PDE
 - The scheme should also easily handle the odd edge shape
- Lagrangian ODE scheme (particle-in-cell)

The XGC1 code

- ODE based Particle-In-Cell approach on configuration space grid
 - Uses unstructured triangular grid
 - Aided by PDE and v-space grid approaches when advantageous
- 5D gyrokinetic equations
 - ODE
 - Time advancement of marker particles
 - Finite difference (PETSc)
 - Partial integro-differential Fokker-Planck collision operator discretized on rectangular v-space grid
 - PDE (PETSc)
 - Maxwell's equations on unstructured triangular x-space grid
- The usual interpolation issue exists

XGC1 contains all the basic physics components

- Gyrokinetic ions
- Drift-kinetic electrons: small gyroradius limit
- Monte-Carlo neutral particle with wall-recycling coefficients (DEGAS2 is built into XGC1)
- Multi-species impurity particles
- Plasma heating in the core
- Torque input in the core
- Fully non-linear Coulomb collisions (Fokker-Planck-Landau)
- Logical Debye-sheath: code determines wall sheath from ambipolar loss constraint.
- Reads in an experimental geometry and plasma data

XGC1 is studying all the critical edge physics

- We normally simulate the whole volume with a coarse grained mesh in the core to capture the large scale turbulence interaction between core and edge.
 - When we confine the simulation to the edge, by placing a core-edge boundary, the turbulence solution gets distorted.
- Use a realistic BD condition for torus: $\Phi=a$ on the wall.
- L-H transition is being studied.

- Edge potential forms spontaneously and the edge pedestal grows, with ionization of wall-recycled neutrals.
- Inward pinch of cold particles found
- Agreement with experimental pedestal profile is excellent

XGC1 has simulated for the first time the nonlinear coherent potential & density structures ("blobs") across separatrix at outside midplane

- Edge rotation source has been identified as a toroidicity effect, but the inward transport has been identified as turbulence effect.

VI. Edge Localized Mode Simulation in M3D

- A large scale Edge Localized Mode (ELM) could make the pedestal crash and send the plasma energy to the material wall → Premature damage to wall, potentially severe under fusion-burning conditions
- Presently, a gyrokinetic code cannot simulate a large scale ELM
- Many observed properties of ELM crash can be explained with MHD
 - Addition of kinetic information could be important. Presently, two-fluid information is used, but edge plasma is kinetic.

Plans and Challenges

- Figure shows an ELM instability event from M3D in a DIII-D plasma
 - Cut-plane view of density contours (blue-green-purple) shows large "fingers" being expelled towards the wall at top and bottom.
 - Top and bottom have magnetic X-points that form near-Hamiltonian "homoclinic" tangles for small perturbations
 - Two 3D density contours (blue and purple) show helical striations along equilibrium magnetic field
 - Edge disturbances couple strongly to the plasma interior
 - Velocity streamlines (3 starting values near outer midplane) show instability motion and gradual development of coherent rotation
- Full understanding of ELMs requires coupling of MHD to particles, which have different physics and computational structures
 - Different time scales, velocities, electric field, etc.
 - Fluid-based MHD solutions are globally coupled, depend on boundary conditions - do not parallelize well on present systems! Particles have more local dynamics, parallelize well.
- Tight coupling (every few time steps) to resolve physics differences.
 - MHD code computes magnetic field B, passes to particle code
 - Particle code computes particle pressure tensor or current density for MHD momentum equations. Challenge: accurate calculation of small velocity moments from particles
 - Main challenge: How to couple codes efficiently on leadership class HPC between non-scalable and scalable codes?

Further Development of XGC1 and Challenges

- Electromagnetic turbulence capability**
 - XGC1 currently can handle perturbative electromagnetic turbulence in a thermal-equilibrium plasma background; called "delta-f" simulation
 - Edge plasma is in non-equilibrium state. The perturbative delta-f capability needs to be upgraded to "full-f."
 - Needs support for parallel unstructured meshing
- Inclusion of 3D perturbed field penetration capability in XGC1 to understand the control of Edge Localized Modes**
 - We presently have this capability without turbulence
- Verification of large scale code**
 - There is no other codes with the capability of XGC1 for cross-verification
 - Analytic solution is difficult due to nonlinear self-organization nature
 - Even a manufactured solution is difficult due to the toroidal mode coupling
 - Verification in a simplified problem must be cleverly designed
- Uncertainty quantification of large scale code is a challenge**
 - UQ also requires a cleverly designed simplified problem set
- Achieve good strong scaling to shortest length electromagnetic turbulence-physics grid in ITER on a heterogeneous platform**
 - A longer term challenge since we do not foresee immediate necessity for such a study
- Prolongation of XGC1 simulation to experimental edge evolution time scale via a multi-scale time advance technique**
 - In memory coupling between coarse and fine grained kernels.
 - Strong collaboration among physics, applied mathematicians, and data management scientists is a critical necessity

UQ Analysis Plan

We are introducing key UQ methodology into the simulation workflow, using DAKOTA and QUESO.

- Improved UQ in derived XGC1 inputs and validation observables: Sampling methods for profile smoothing, EFIT and TRANSP outputs
- Forward sensitivity analysis of temperature and density profiles to key XGC1 inputs (heating power, neutral recycling rate, magnetic field geometry) and physics choices (various turbulence modes, impurity)
- Bayesian calibration of reduced-physics models (anomalous transport model in XGC0)

Profile Smoothing/Fitting

- Apply UQ not only to XGC1, but also to experimental validation data
- Automated profile smoother, using bivariate space-time splines with sawtooth binning (AIC, BIC for spline properties)
- Use DAKOTA to benchmark MC and Latin Hypercube Sampling (LHS) profile fitting
- LHS showed improved convergence rate, variance reduction
- Reducing sample size important when extended to more expensive "samples": outputs from EFIT or TRANSP
- Currently under extension to other codes, sampling methods (ILHS)

Challenges: Poor uncertainty models for inputs to diagnostic routines, incorporating data from other diagnostics into fitting routines, core and edge constraints

XGC1 Sensitivity Analysis

Currently we are evaluating sensitivity of key 1D physics profiles ($T_{e,n}$) and their gradients to model parameters (heating and cooling) and numerics (timestep size, particle number, spatial grid size).

- Dedicated UQ branch of XGC1 software repository with access to main branch XGC1 routines, scripting support for interface with UQ tools
- Currently exploring simplified ITG physics as a reduced model allowing sufficient UQ sample size
- Incremental process of adaptively enriching the model when indicated by experimental data

Challenges: Balancing computational demands of full-physics simulation versus sampling demands of UQ, developing UQ analysis to extrapolate from simplified to more complex physics models, treatment of sampling bias due to numerical artifacts

Calibration of Reduced Model in XGC0

- Goal:** Bayesian calibration of anomalous transport model using H-mode DIII-D data in reduced physics (XGC0) using QUESO
- Similar process potentially applicable to calibration of XGC1 inputs
- Challenges:** General XGC1 extension may lead to a large, expensive inverse problem

4X Performance Improvement at Scale

Optimization of distributed memory and shared memory parallel algorithms and porting of computational kernel to GPU accelerator improved computer performance over the January 2013 CPU-only version by a factor of between 3.5 and 4.5 for problem sizes of scientific interest (≈ 8192 compute nodes in weak scaling study) on Cray XK7 Titan at the Oak Ridge Leadership Computing Facility.

- The computational kernel for simulating trajectories for electrons (PUSHE), which accounts for > 85% of the overall run time for the optimized CPU-only version, is the initial target for optimizing execution using the GPU
- GPU kernels are generated using the PGI CUDA Fortran compiler, while OpenMP is used to exploit parallelism on the multi-core CPU.
- The particle workload is partitioned between the GPU and the multi-core CPU on each compute node. Using just the GPU for PUSHE is between 2.5 and 2.7 times faster than using just the multi-core CPU. An assignment of 74% of particles to the GPU and 26% to the CPU cores optimizes performance, and is between 3.1 and 3.5 times faster than using just the multi-core CPU.

Performance: Next Steps

- Electrons have higher velocities than ions and can cross multiple subdomains in each ion time step. To enable PUSHE to proceed without MPI communication, the global electric field is replicated on each GPU. For high resolution electromagnetic simulation of ITER, this will be difficult. The memory requirement can be reduced by a factor of 6 if only the potential is replicated and the field components are computed on the GPU as needed.
- To avoid collisions in update operations, certain arrays are replicated. On the GPU this leads to large memory requirements when thousands of threads are used. Alternative implementations are being developed that exploit the recently available efficient atomic update operations on 64-bit floating-point values, lowering memory requirements and allowing more threads to be launched, hopefully improving performance.
- New science capabilities will require a 2D domain decomposition to partition grid and particles ("poloidal decomposition") instead of the current 1D domain decomposition and random partition of particles in other dimensions. New capabilities will change the performance characteristics significantly, but experiments using the current version indicate a computational load imbalance on the GPU not related to imbalance in number of particles. Non-power-of-two MPI collectives also appear to demonstrate poor performance at scale for multiple MPI tasks per node.

Manual calibration of 5 parameter anomalous transport model yielding promising results (D. Battaglia)

Tight Code Coupling

ADIOS (2013 R&D 100 winner) has been developed to provide low-latency code coupling in EPSI simulation to support tightly coupled execution scenarios. The main focus of the development is to provide:

- Low-latency, tight coupling execution environments through memory-to-memory data exchanges between different codes/executions
- Service Oriented Architecture (SOA) for on-demand coupling executions with support of dynamic workflow invocation
- Coupling executions in heterogeneous computing environments

Evolution of coupling

Past approach: Kepler + ADIOS

- File-based code coupling resulted in high latency, low-throughput, and under-utilization of resources.
- Static workflow demanded lots of human efforts in designing and updating workflows.
- Customized applications with hard-coded execution plan.

Paradigm shift: ADIOS + embedded workflows

- Support efficient memory-to-memory/in-memory multi-code coupling (e.g., using DataSpaces).
- Semantic-rich, machine-readable information embedded in data
- Flexibility in coupling execution.

Data-centric integrated execution environment

Our focus is to support EPSI by providing integrated data-centric execution environments for tight code coupling, staged data process, and monitoring system with a support of dynamic workflow system

Data Staging

Recent ADIOS release (version 1.5) with DataSpaces has been incorporated in EPSI simulations to support efficient I/O operations:

- Streaming data
- Non-blocking operations
- Selection and chunked reads to enable schedule optimization
- Staging with a unified API set for file and in-memory coupling
 - Maintain backward compatibility
 - Read data from files or memory with a unified API

Hybrid staging

- Hybrid approach to deal with exploding data volume
- Open questions on using GPUs and SSDs
- Asynchronous decoupled analysis for faster time to solution
- Enables online in-situ/in-transit data processing, and asynchronous memory-to-memory data sharing for coupled simulation workflow

Graph of data transfers between coupled codes

Unstructured Meshing

Methods and tools for XGC unstructured meshes – Efforts include:

- Generation of better meshes meeting constraints
 - Control of element shapes and gradation
 - Maintain aligned mesh layers between curves of constant flux on interior (and exterior if possible)
- Introduce increased flexibility around x-point and at geometric features at outer walls
- Parallel mesh and particle
 - Currently have a copy of mesh on each core – potential scaling and memory issue
 - Evaluating using FASTMath PUMI parallel mesh to control parallel mesh and particle methods
- Controlling errors on transfer of data between particles and mesh
 - Error sources include:
 - Linear mesh edges approximating curved flux surfaces
 - Mesh spacing between flux surfaces not assuming piece-wise linear while actual variation is non-linear
 - Piece-wise linear approx. over elements covering many particles
 - Errors inherent to use of different "basis" in two methods
 - Error reduction options – finer and/or higher order (curved) meshes

Multi-scale Time Advancement

- Prolong the high fidelity simulation to experimental time scale (~50 ms)
- Expensive turbulence simulation may not be needed at all time steps
- Reset error accumulation in the way
- Divide XGC1: XGC²(axisymmetric-turbulence) and XGC³(axisymmetric)
- Use Φ^2 (turbulence) in XGC³, with updates as needed
- Requires collaboration with Math, DM, UQ, and Optimization scientists

Accomplishments

- Developed a detailed strategy for coarse/fine grain coupling to encode turbulent information in the coarse grained simulation.
- Developed a coarse grained XGCa from XGC1, and demonstrated data coupling with XGC1.
- Identified a strongly turbulent benchmark case to help guide the development of strategies for adaptive multi-scale advancement.

Challenges and next steps

- Identify and understand appropriate measures of quality of the simulation and validate against fully resolved simulations to quantify the impact of the multi-scale approach on the physical fidelity.
- Study physically correct sampling of particles when coupling the two codes to minimize the transitional effects, e.g., phase space density reconstruction and conditional sampling techniques.
- Strategies for stiff profile evolution and solution bifurcation.
- Develop algorithm to determine the coupling time steps.
- Strategies for V&V and UQ.

Solvers

- Scalable Poisson-type Solvers – next steps
 - Continue to develop non-linear solver for Boltzmann electrons
 - Scale linear solver to strong scaling limit for exascale machines
 - Amper's Law solver with electromagnetic perturbations
 - Higher order interpolation & high-order discretizations
 - Solve full gyrokinetic field equations with flux-surface averaging:
 - Formulate with auxiliary variable and ...
 - Use PETSc's FieldSplit solvers
 - Add auxiliary variable for flux surface average: $-\Delta\phi + (\phi - \langle\phi\rangle) = \rho$
- FMM-like solvers for screened potential problems
 - FMM-accelerated solver for variable coefficient and non-linear Poisson problems
- 3D FMM based solvers for electrostatics and electromagnetics
- Performance optimization on exascale

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