

# Scidac 2015 progress: Advanced Modeling of ions in solutions, on surfaces, and in biological environments

Princeton University: **Roberto Car (PI)**, Weinan E

Temple University: Mike Klein, **Xifan Wu (presenting)**

LBL: Esmond Ng, Chao Yang, Lin Lin



## **Part I. Projects**

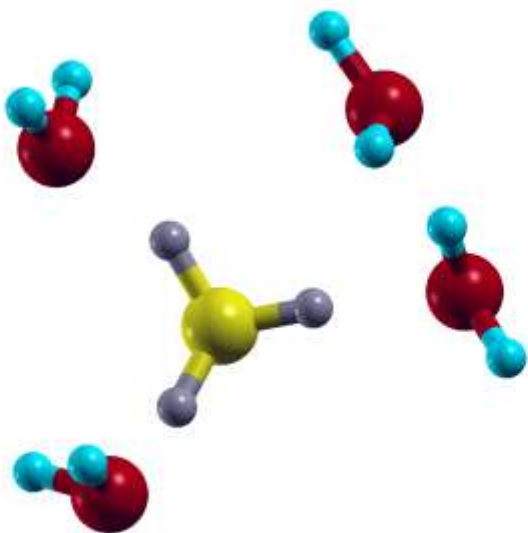
- **Proton transfer of OH<sup>-</sup> and H<sub>3</sub>O<sup>+</sup> in an accurately modeled H-bond network**
- **X-ray absorption spectra in liquid water by advanced modeling**

## **Part II. Progress of our team members at LBL**

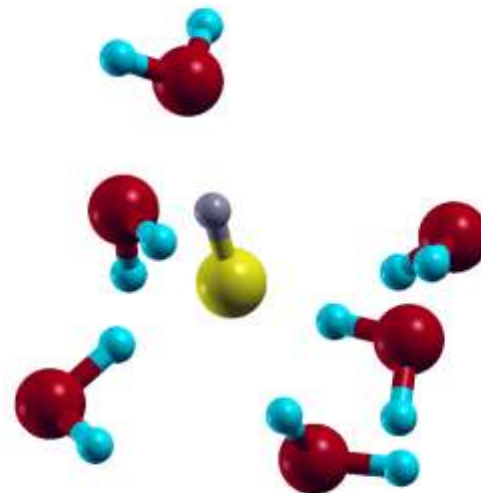
## **Part III. Other performed projects and introduction of our posters**

# Proton Transfer through hydronium and hydroxide: Current controversy

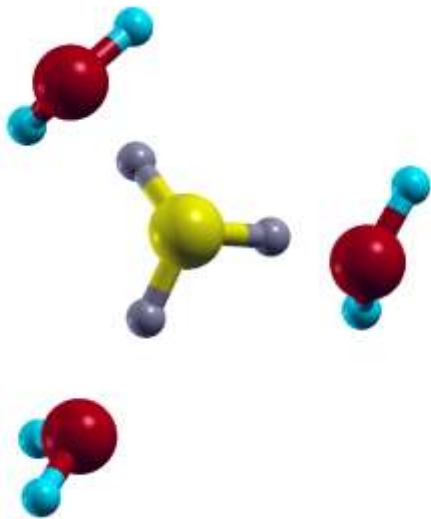
PT in  $\text{H}_3\text{O}^+$  through structural diffusion



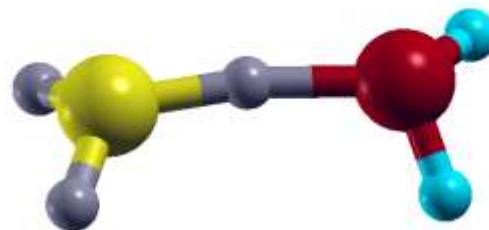
PT in  $\text{OH}^-$  through structural diffusion



Proton Transfer mechanism in  $\text{H}_3\text{O}^+$



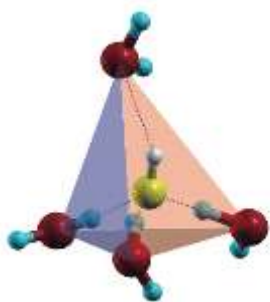
Eigen cation



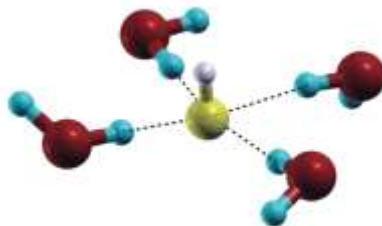
Zundel cation

## Three controversial mechanisms for hydroxide OH-

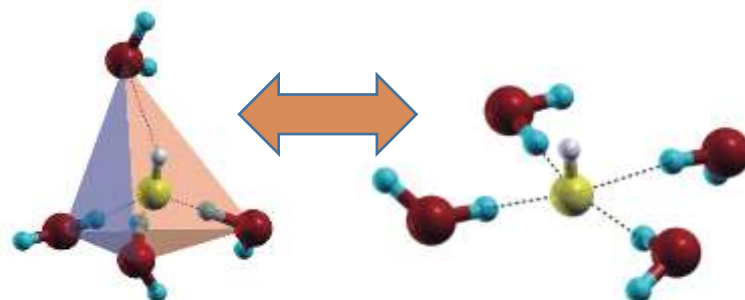
Mirror image



Static hyper-coordination



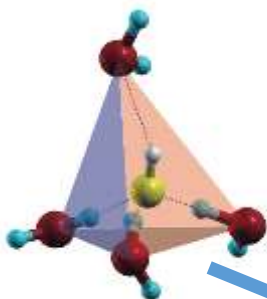
Dynamical hyper-coordination



# Proton Transfer through hydronium and hydroxide

## Three controversial mechanisms for hydroxide OH-

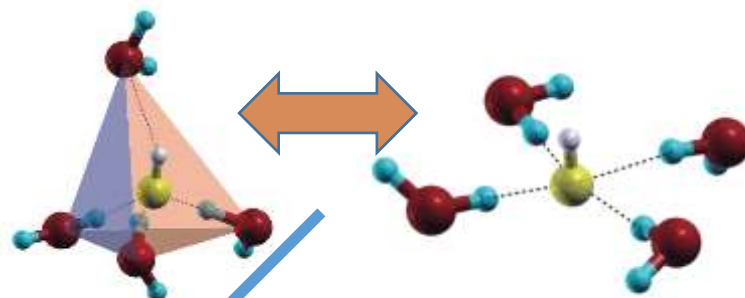
Mirror image (MI)



Static hyper-coordination (SH)



Dynamical hyper-coordination (DH)



Diffusion Coefficient ( $10^{-9}$ m <sup>2</sup> /s)	MI(PW91) <sup>1</sup>	SH(HCTH) <sup>1</sup>	DH (BLYP) <sup>1</sup>	Exp. <sup>2, 3, 4</sup>
OH <sup>-</sup>	18.5	0.44	<b>1.92</b>	3.12
H <sub>3</sub> O <sup>+</sup>	3.24	3.25	<b>2.83</b>	6.69
D(OH <sup>-</sup> )/D(H <sub>3</sub> O <sup>+</sup> )	5.88	0.14	<b>0.68</b>	0.47

### Why controversial?

- All three scenarios can be theoretically obtained by GGA functional
- BLYP predicts a qualitatively correct picture, but ions diffuse too slow
- The H-bond by BLYP is known to be over-structured

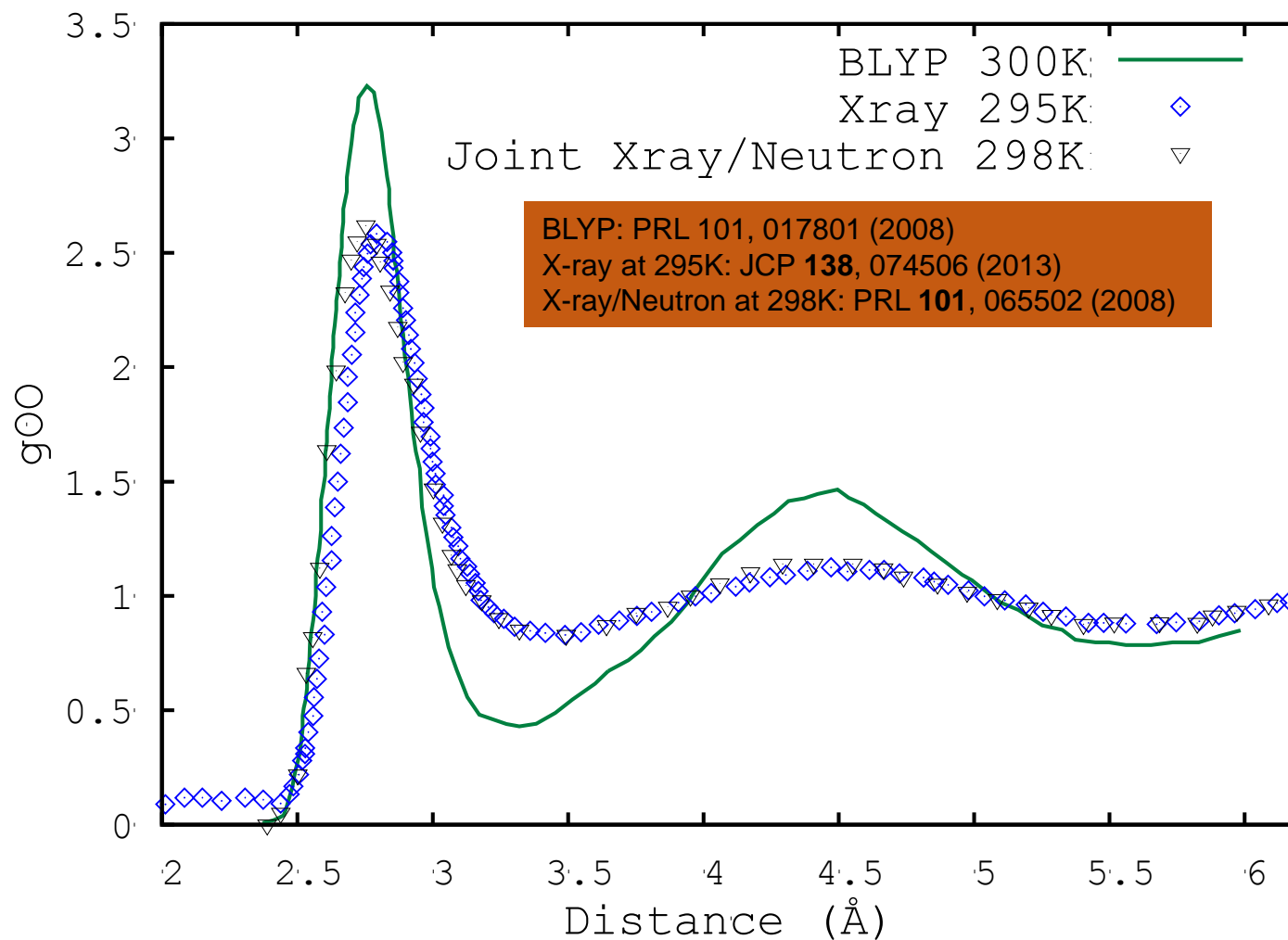
1. Tuckerman, M. E.; Chandra, A.; Marx, D. *J. Chem. Phys.* 133, 124108 (2010)

2. Tuckerman, M. E.; Chandra, A.; Marx, D. *Chem. Rev.* 2010, 110, 2174

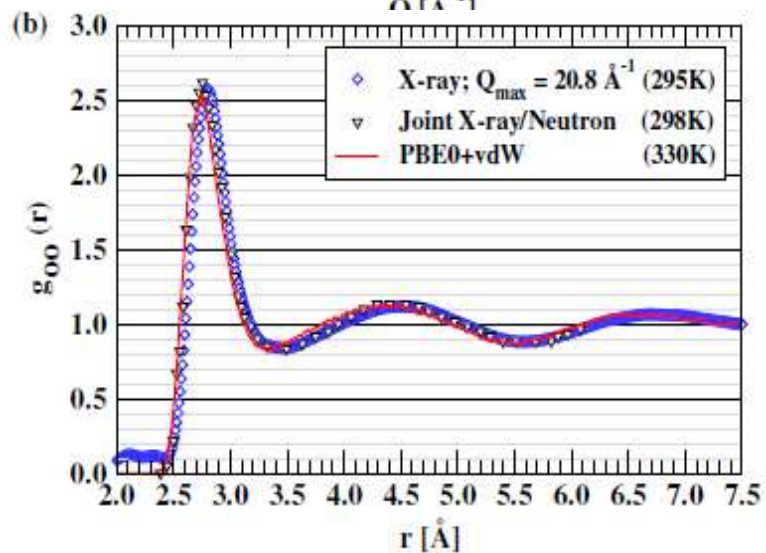
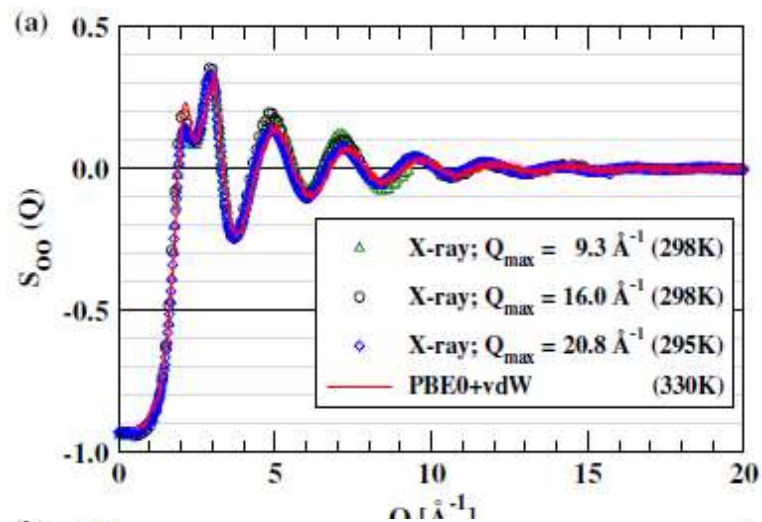
3. Milles, R. *J. Phys. Chem.*, 1973, 77, 685

4. Halle, B.; Karlstrom, G. *J. Chem. Soc., Faraday Trans. 2* 1983, 70, 1031

# Proton Transfer through hydronium and hydroxide: Current controversy



# Proton Transfer with accurately modeled H-bond network



**Accurate modeling of H-bond is the key!!**

What are missing in GGA-AIMD simulations?

- Inclusion of van der Waals interactions
- Correction of delocalization by hybrid functional
- Treatment of nuclear quantum effects

Our advanced modeling approaches:

- TS-vdW
- PBE0 hybrid functional
- Approximate treatment of nuclear quantum effect by 30K elevated temperature



## Diffusion

Diffusion Coefficient ( $10^{-9}$ m <sup>2</sup> /s)	BLYP <sup>1</sup>	PBE	PBE vdW	PBE0 vdW	Exp. <sup>2, 3, 4</sup>
OH <sup>-</sup>	1.92	16.4	14.0	<b>3.90</b>	3.12
H <sub>3</sub> O <sup>+</sup>	2.83	9.78	11.4	<b>8.15</b>	6.69
D(OH <sup>-</sup> )/D(H <sub>3</sub> O <sup>+</sup> )	0.68	1.7	1.2	<b>0.48</b>	0.47

## Proton Transfer rate (per picosecond)

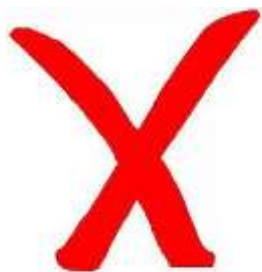
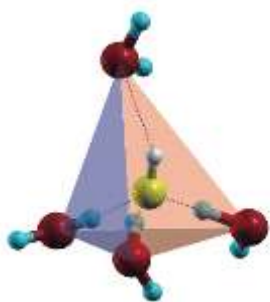
PT rate	PBE	PBE vdW	PBE0 vdW
OH <sup>-</sup>	2.92	2.26	0.607
H <sub>3</sub> O <sup>+</sup>	2.06	2.78	1.90

1. Tuckerman, M. E.; Chandra, A.; Marx, D. *J. Chem. Phys.* 133, 124108 (2010)
2. Tuckerman, M. E.; Chandra, A.; Marx, D. *Chem. Rev.* 2010, 110, 2174
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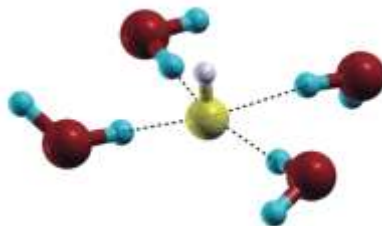
## OH<sup>-</sup>

Three controversial mechanisms for hydroxide OH<sup>-</sup>

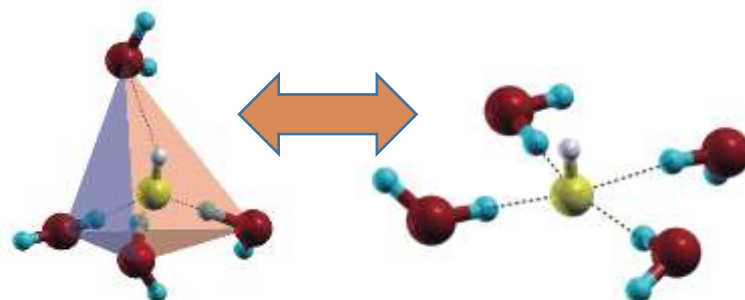
Mirror image



Static hyper-coordination

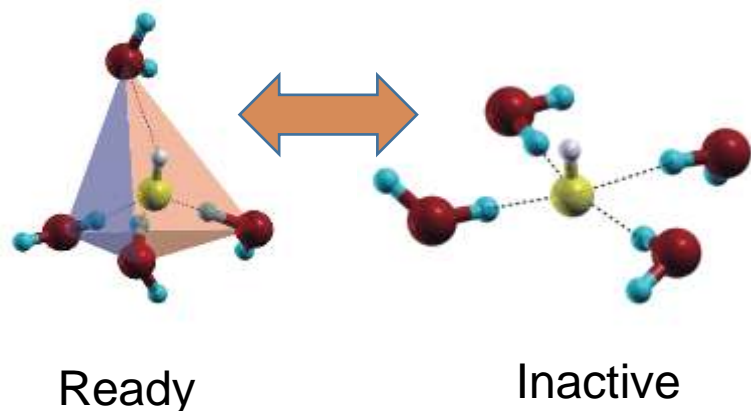


Dynamical hyper-coordination



## OH<sup>-</sup>

Dynamical  
hyper-coordination



Presolvation structure of PT in OH<sup>-</sup>:

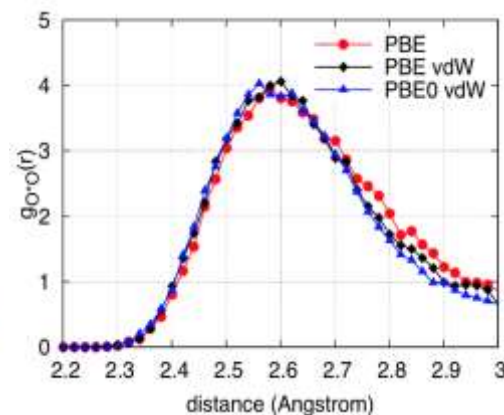
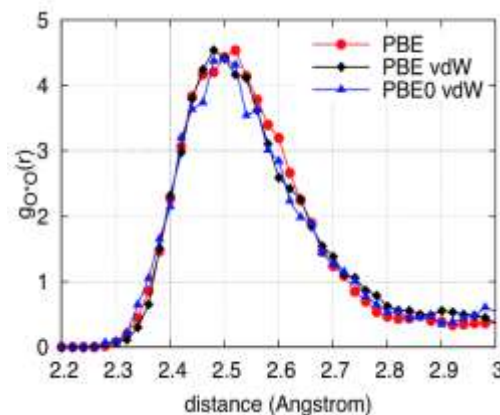
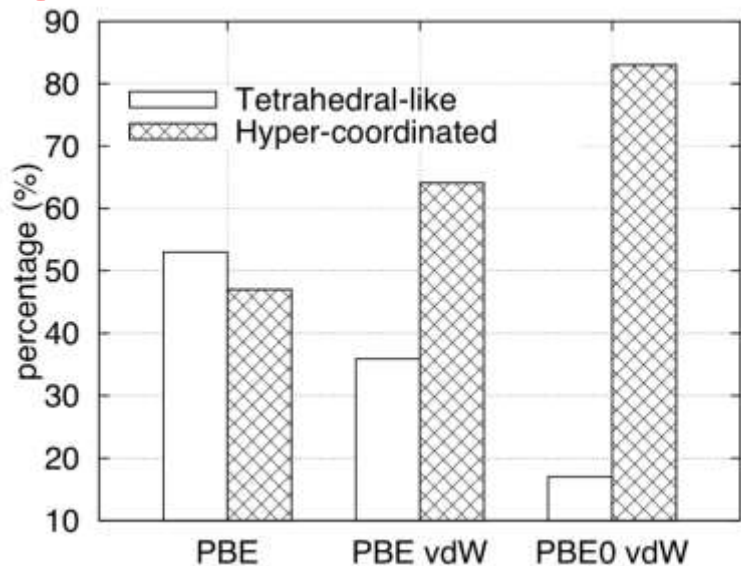
- Complex receiving the proton
- Resembling water
- Must change from hypercoordination to tetrahedral like

Diffusion Coefficient (10 <sup>-9</sup> m <sup>2</sup> /s)	BLYP <sup>1</sup>	PBE	PBE vdW	PBE0 vdW	Exp. <sup>2, 3, 4</sup>
OH <sup>-</sup>	1.92	16.4	14.0	<b>3.90</b>	3.12

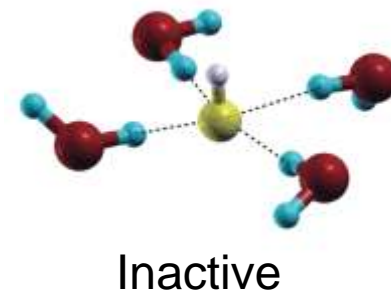
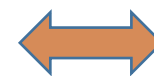
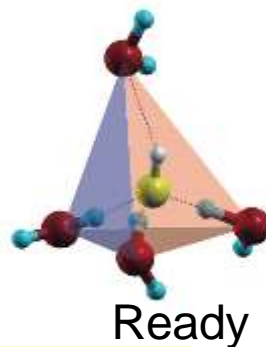
1. Tuckerman, M. E.; Chandra, A.; Marx, D. *J. Chem. Phys.* 133, 124108 (2010)
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3. Milles, R. *J. Phys. Chem.*, 1973, 77, 685
4. Halle, B.; Karlstrom, G. *J. Chem. Soc., Faraday Trans. 2* 1983, 70, 1031

# Proton Transfer of OH<sup>-</sup>: Presolvation structure

## OH<sup>-</sup>



Dynamical  
hyper-coordination

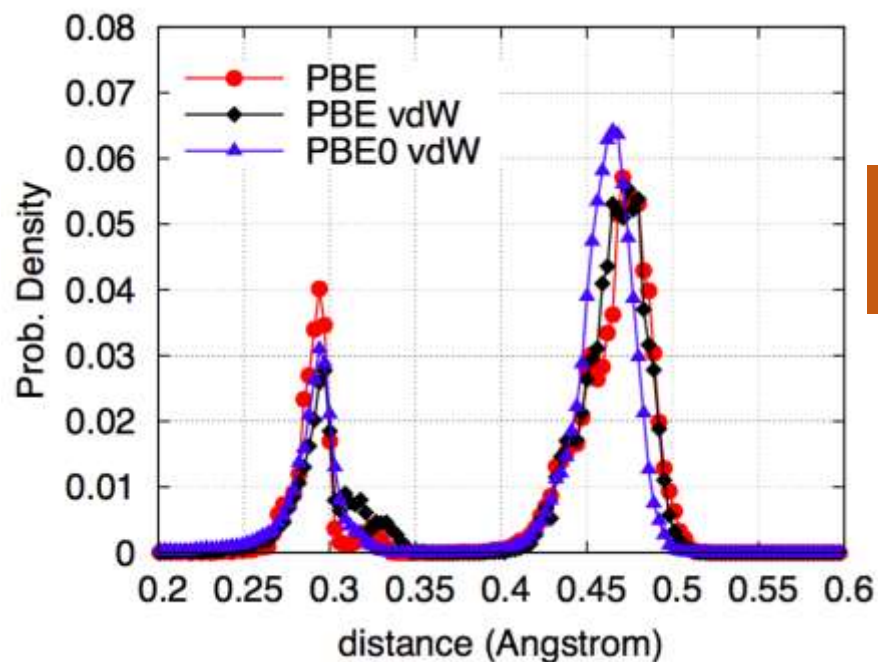


1. Tuckerman, M. E.; Chandra, A.; Marx, D. *J. Chem. Phys.* 133, 124108 (2010)
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Diffusion Coefficient ( $10^{-9}$ m <sup>2</sup> /s)	BLYP <sup>1</sup>	PBE	PBE vdW	PBE0 vdW	Exp. <sup>2, 3, 4</sup>
OH <sup>-</sup>	1.92	16.4	14.0	<b>3.90</b>	3.12

# Proton Transfer with accurately modeled H-bond network

## OH<sup>-</sup>



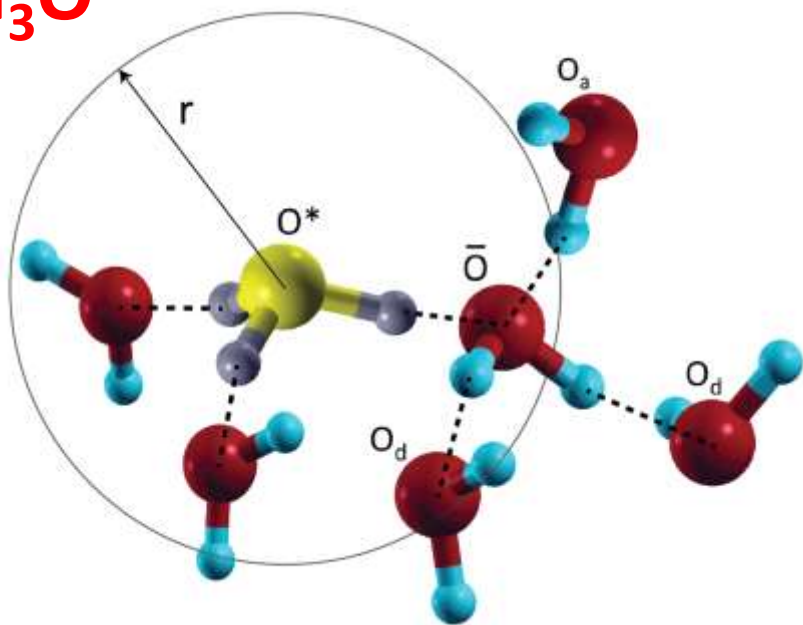
**Weakening of directional H-bond strength !**

Diffusion Coefficient ( $10^{-9}$ m <sup>2</sup> /s)	BLYP <sup>1</sup>	PBE	PBE vdW	PBE0 vdW	Exp. <sup>2, 3, 4</sup>
OH <sup>-</sup>	1.92	16.4	14.0	<b>3.90</b>	3.12

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L. Zheng, B. Santra, R. DiStasio Jr., R. Car, M. Klein, X. Wu, manuscript in preparation

# Proton Transfer with accurately modeled H-bond network



Presolvation structure of PT in  $\text{H}_3\text{O}^+$ :

- Complex receiving the proton
- Water molecule in first shell
- A2D2 (inactive) to A1D2 (ready)

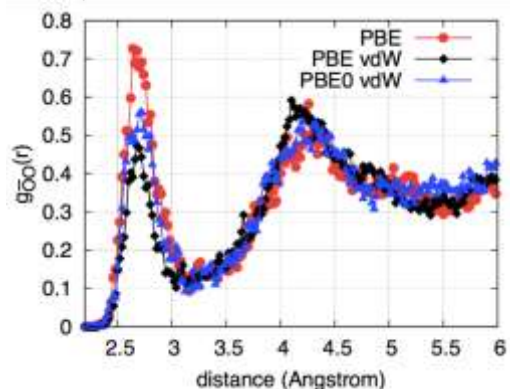
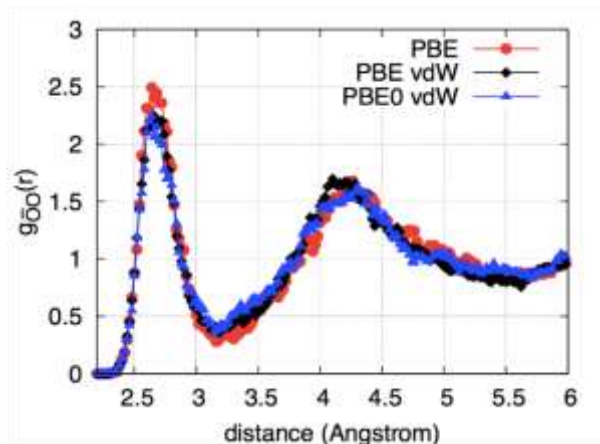
Diffusion Coefficient ( $10^{-9} \text{ m}^2/\text{s}$ )	BLYP <sup>1</sup>	PBE	PBE vdW	PBE0 vdW	Exp. <sup>2, 3, 4</sup>
$\text{H}_3\text{O}^+$	2.83	9.78	11.4	<b>8.15</b>	6.69

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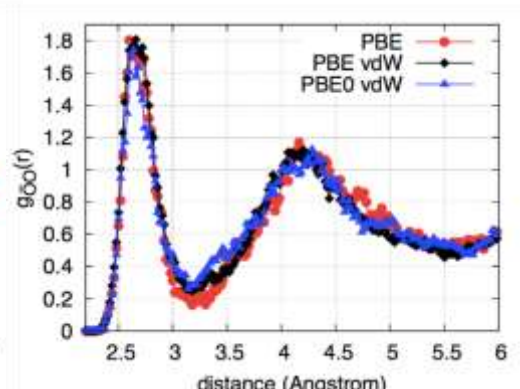
# Proton Transfer with accurately modeled H-bond network



decompose 

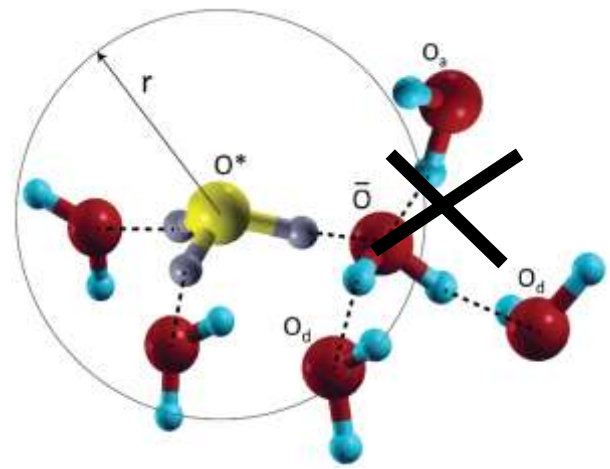


lone pair side

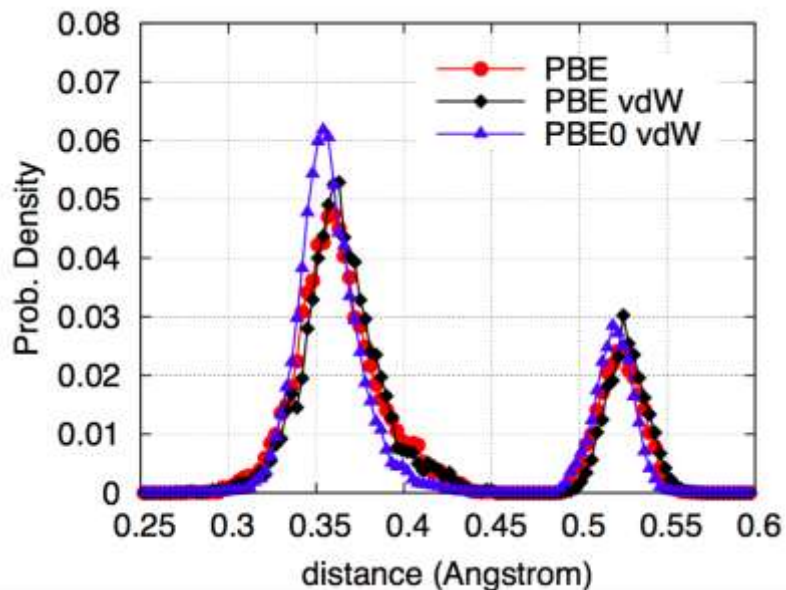


hydrogen side

Functional	Inactive		Ready
	A2D2	A1D2	Others
PBE	64.35	33.47	2.19
PBE_vdW	58.78	35.22	6.00
PBE0_vdW	51.22	41.94	6.84



# Proton Transfer with accurately modeled H-bond network



Functional	Inactive Ready		Others
	A2D2	A1D2	
PBE	64.35	33.47	2.19
PBE_vdW	58.78	35.22	6.00
PBE0_vdW	51.22	41.94	6.84

Diffusion Coefficient ( $10^{-9}$ m <sup>2</sup> /s)	BLYP <sup>1</sup>	PBE	PBE vdW	PBE0 vdW	Exp. <sup>2, 3, 4</sup>
H <sub>3</sub> O <sup>+</sup>	2.83	9.78	11.4	<b>8.15</b>	6.69

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1. Settle down the controversy on the proton transfer mechanism in OH-
2. Delocalization correction by hybrid functional
3. van der Waals interaction
4. Slow down PT in OH- towards experimental direction
5. The PT of H<sub>3</sub>O<sup>+</sup> is much less affected due to error cancelation

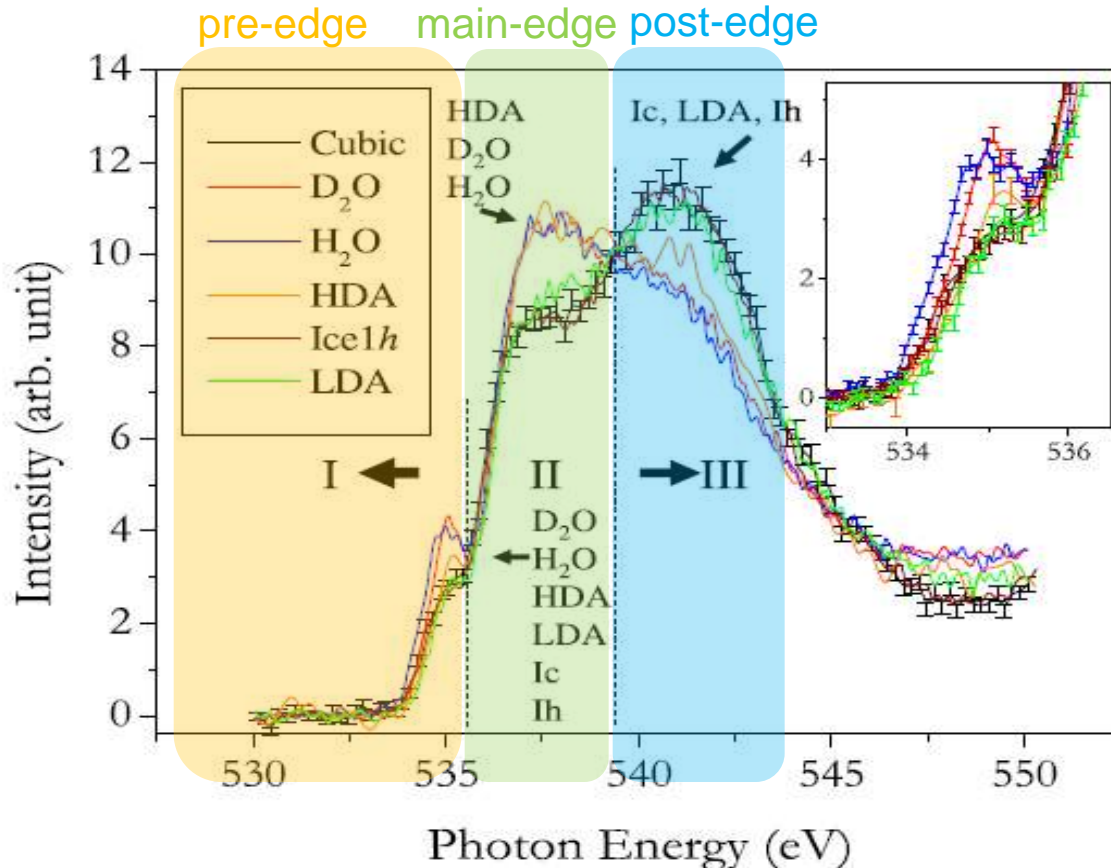
## **Part I. Projects**

- **Proton transfer of OH<sup>-</sup> and H<sub>3</sub>O<sup>+</sup> in an accurately modeled H-bond network**
- **X-ray absorption spectra in liquid water by advanced modeling**

## **Part II. Progress of our team members at LBL**

## **Part III. Other performed projects and introduction of our posters**

# X-ray absorption of liquid water and ice

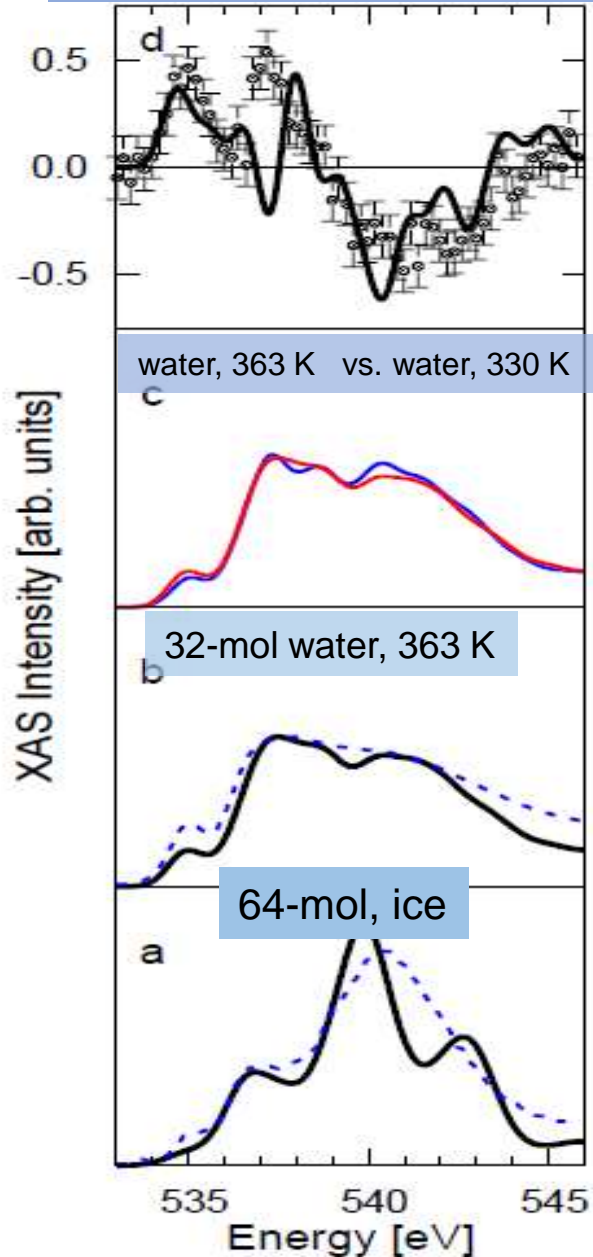


J. Tse *et. al.* Phys. Rev. Lett. 100,095502(2008)

- The spectral width ( $\sim 11$  eV) is the same in all spectra
- Three features (pre-edge, main-edge, post-edge) are present in the same energy range in all spectra
- The relative intensity of the features shows a characteristic system dependence

# X-ray absorption of liquid water and ice

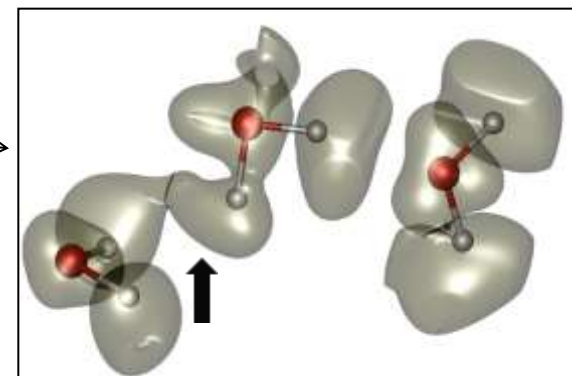
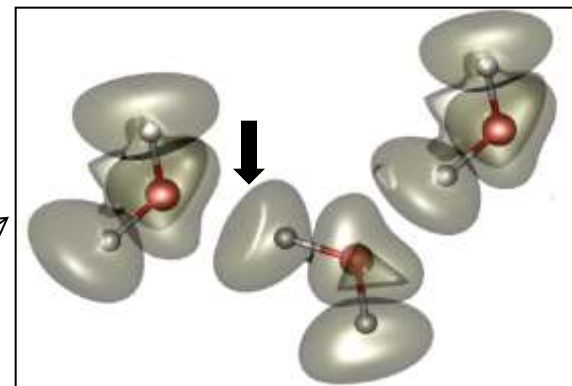
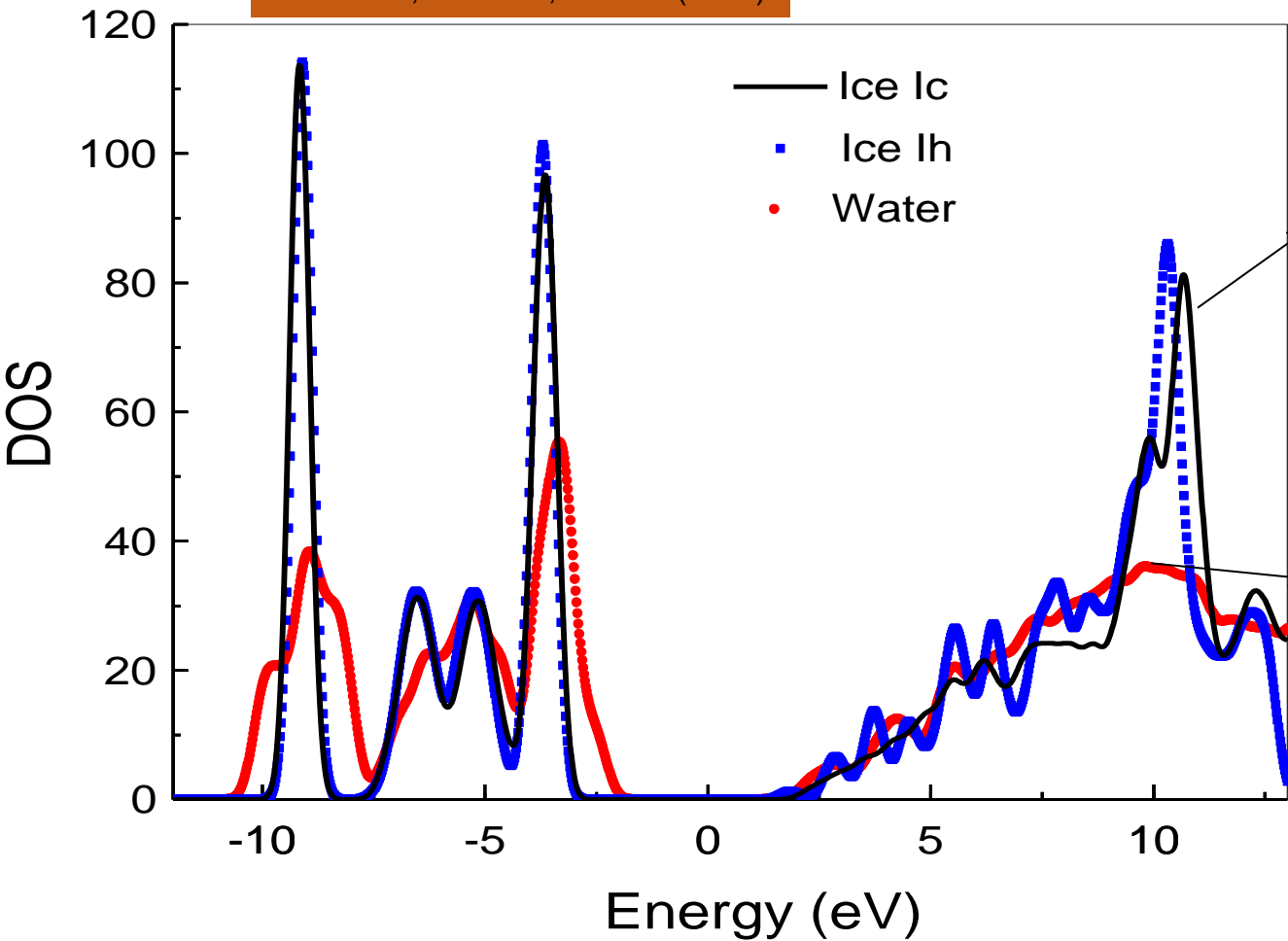
Variation of the spectrum with T



- Quasiparticle treatment based on GW approximation is crucial in obtaining the XAS spectra
- Difference in XAS between water and ice

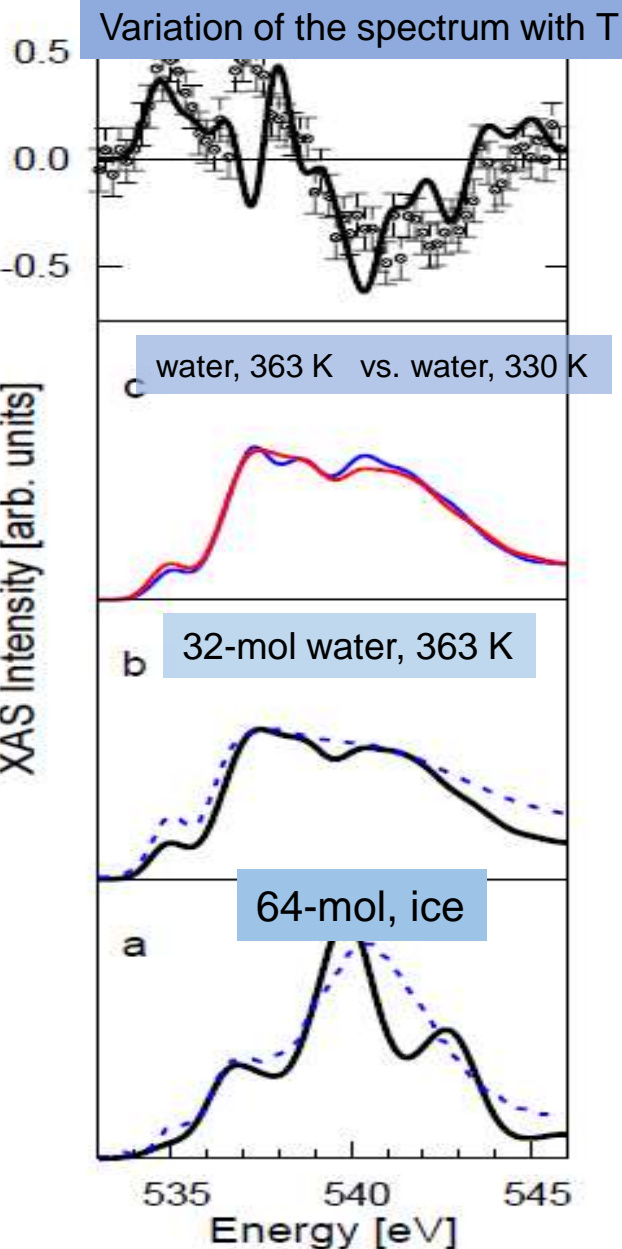
# X-ray absorption of liquid water and ice: the difference in main peak

Chen *et al*, PRL 105, 017802 (2010)



# X-ray absorption of liquid water and ice

Chen *et al*, PRL 105, 017802 (2010)



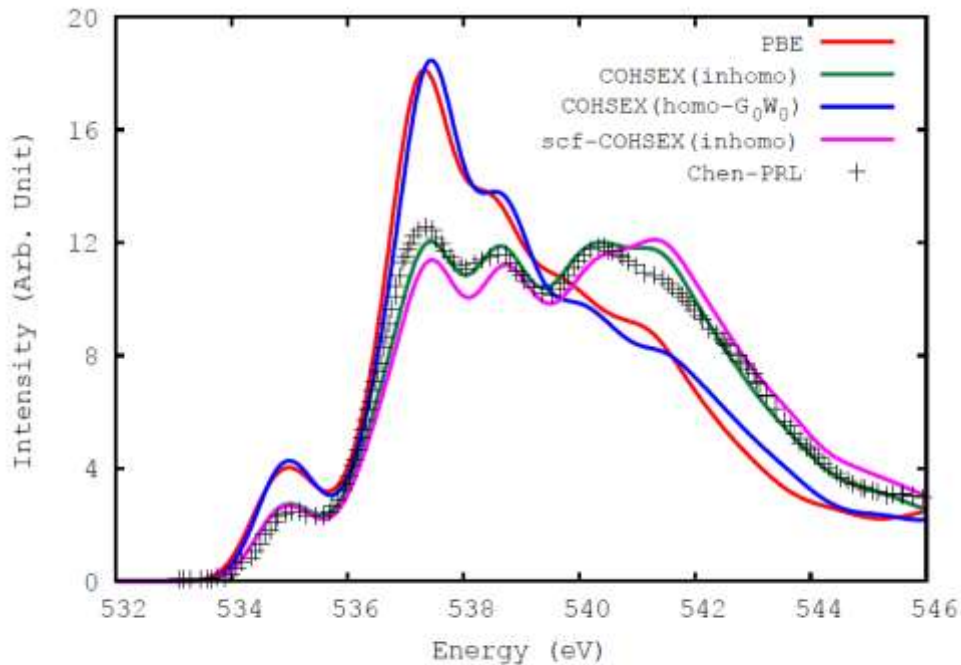
## AIMD: ab initio molecular dynamics

### ➤ Importance of of electron excitation calculations?

- ❖ GW vs. DFT method
- ❖ G0W0 vs self-consistent GW

### ➤ The importance of molecular modeling of water by AIMD?

- vdW and hybrid functional
- nuclear quantum effect
- *ab initio* vs. classical MD
- size effect in water model



Chen *et al*, PRL 105, 017802 (2010)

## AIMD: ab initio molecular dynamics

### ➤ Importance of electron excitation calculations?

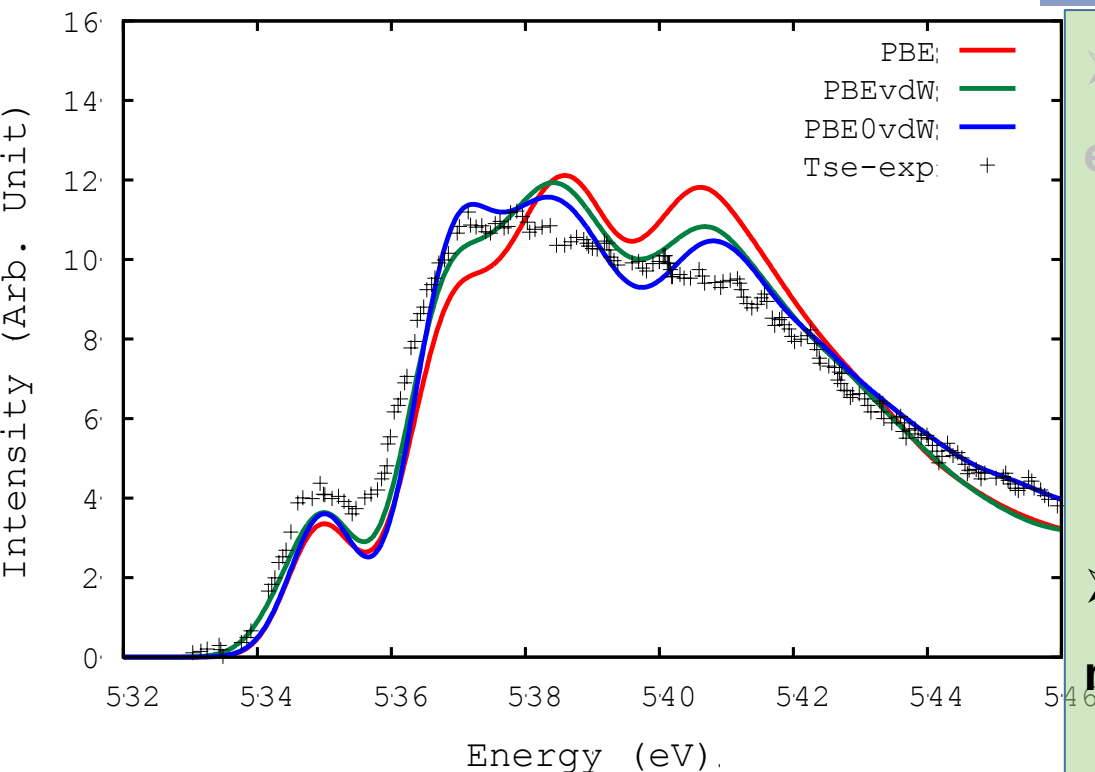
- ❖ GW vs. DFT method
- ❖ **G0W0 vs self-consistent GW**

### ➤ The importance of molecular modeling of water by AIMD?

- vdW and hybrid functional
- nuclear quantum effect
- *ab initio* vs. classical
- size effect in water model

# X-ray absorption of liquid water : recent advanced modeling

Z. Sun, et. al. in preparation



Liquid water modeled in a cubic box of 128-mol

## AIMD: ab initio molecular dynamics

➤ Importance of electron excitation calculations?

- ❖ GW vs. DFT method
- ❖ G0W0 vs self-consistent GW

➤ The importance of molecular modeling of water by AIMD?

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- *ab initio* vs. classical
- size effect in water model



# X-ray absorption of liquid water : nuclear quantum effect

Z. Sun, et. al. in preparation

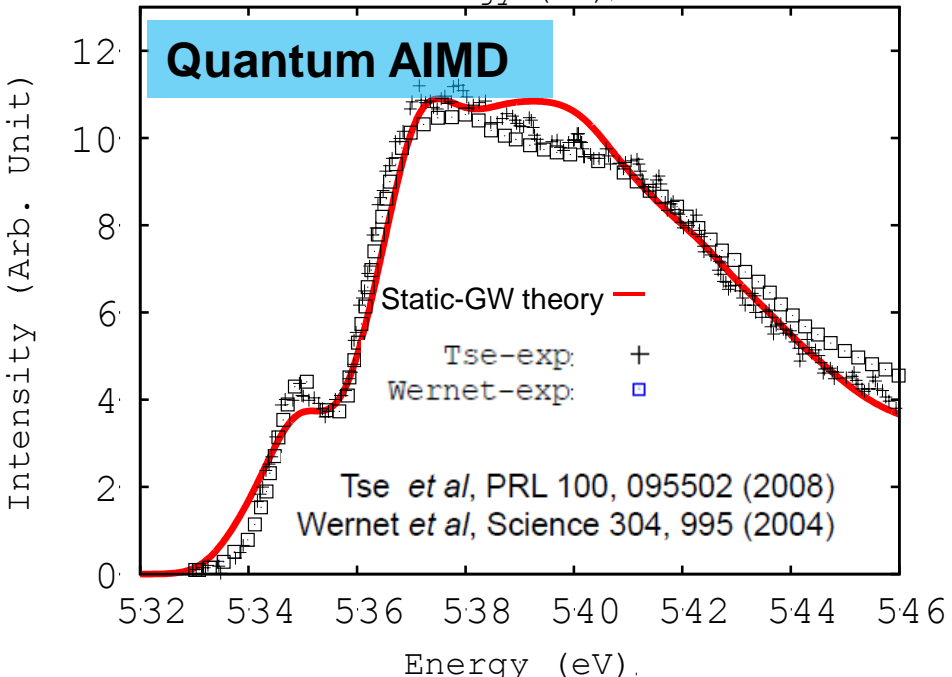
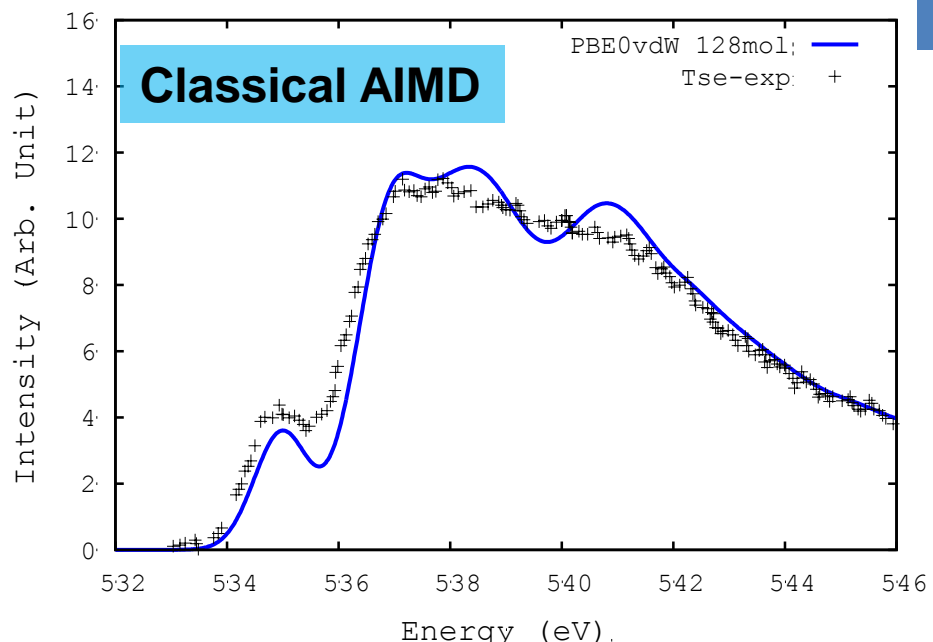
## AIMD: ab initio molecular dynamics

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➤ The importance of molecular modeling of water by AIMD?

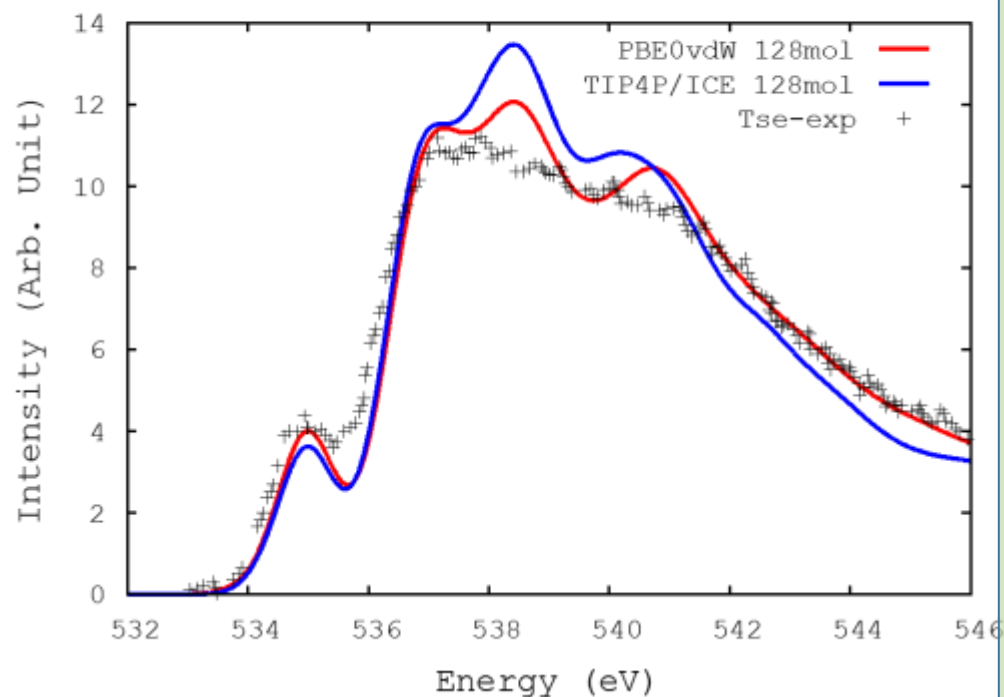
- vdW and hybrid DFT
- **nuclear quantum effect**
- *ab initio* vs. classical MD
- size effect in water model



# X-ray absorption of liquid water : recent advanced modeling

Z. Sun, et. al. in preparation

XAS of 128mol TIP4P/ICE water



Tse et al., PRL 100, 095502 (2008)

## AIMD: ab initio molecular dynamics

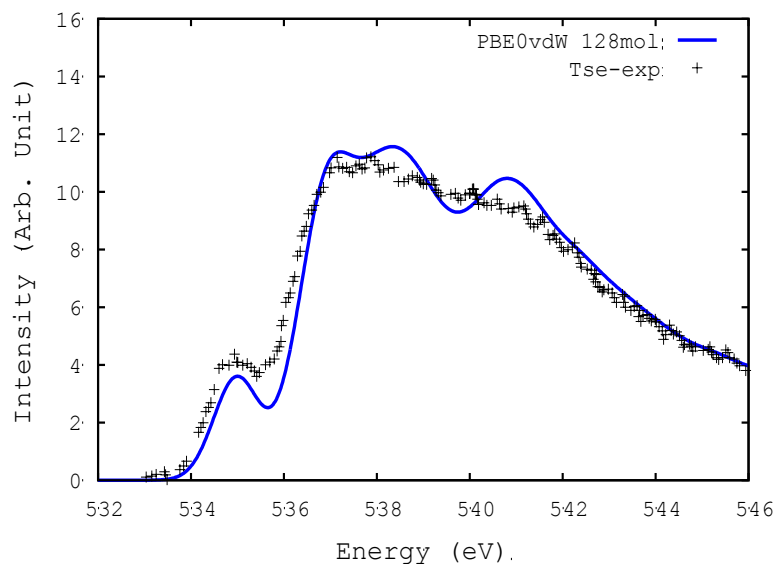
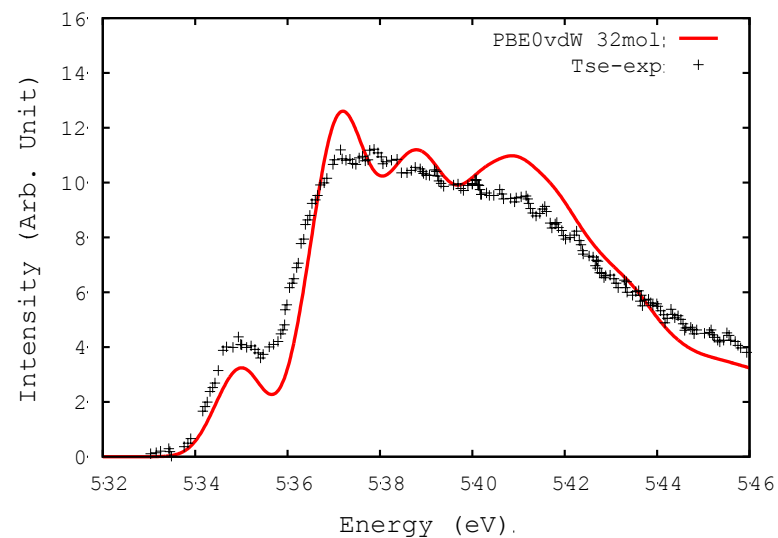
➤ Importance of electron excitation calculations?

- ❖ GW vs. DFT method
- ❖ G0W0 vs self-consistent GW

➤ The importance of molecular modeling of water by AIMD?

- vdW and hybrid DFT
- nuclear quantum effect
- **ab initio vs. classical MD**
- size effect in water model

# X-ray absorption of liquid water : recent advanced modeling



➤ Importance of of electron excitation calculations?

❖ GW vs. DFT method

❖ G0W0 vs self-consistent GW

➤ The importance of molecular modeling of water by AIMD?

○ vdW and hybrid DFT

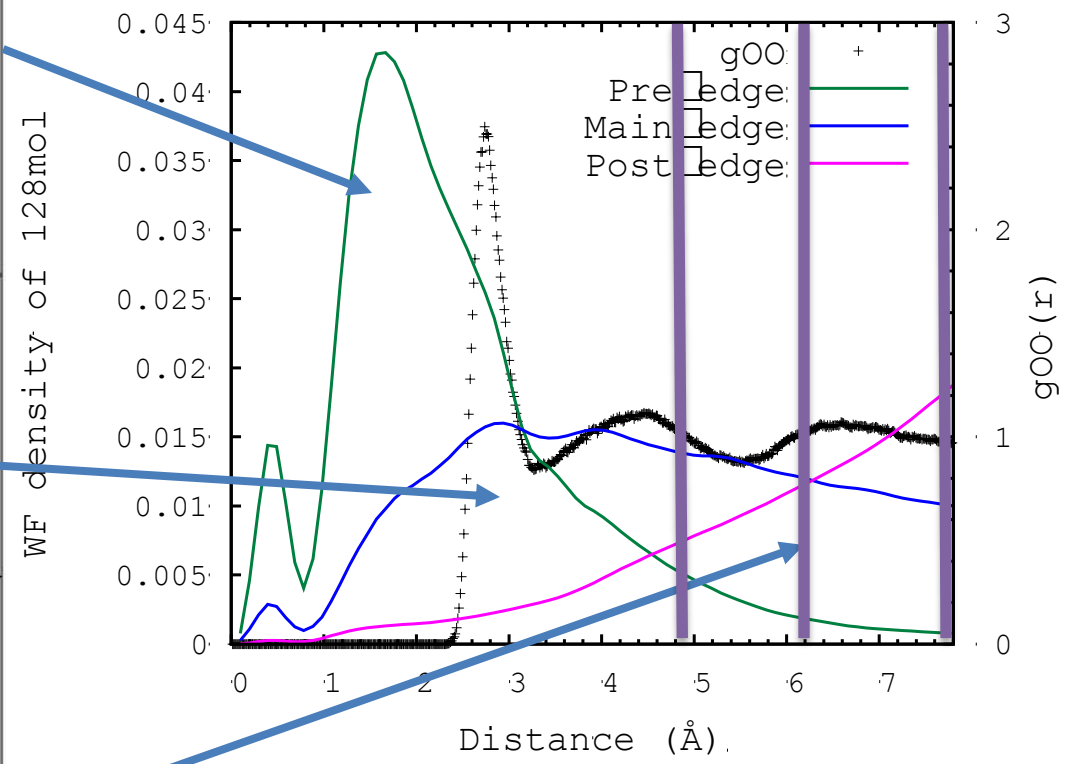
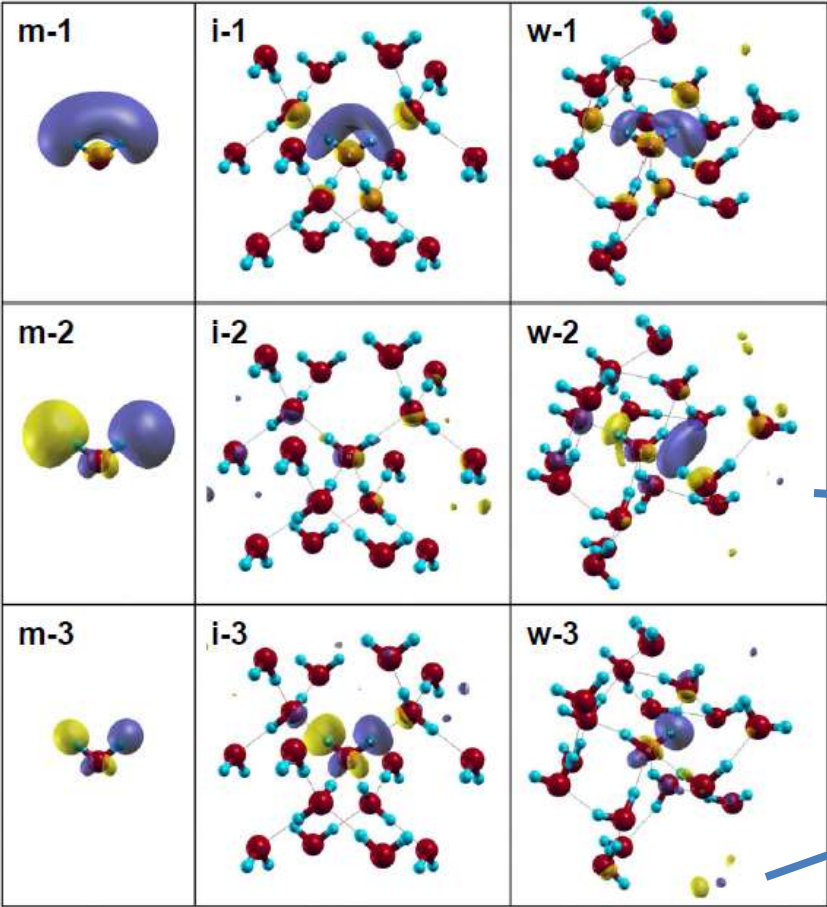
○ nuclear quantum effect

○ *ab initio* vs. classical MD

○ **size effect in water model**

# X-ray absorption of liquid water : advanced modeling

32-mol box	64-mol box	128-mol box
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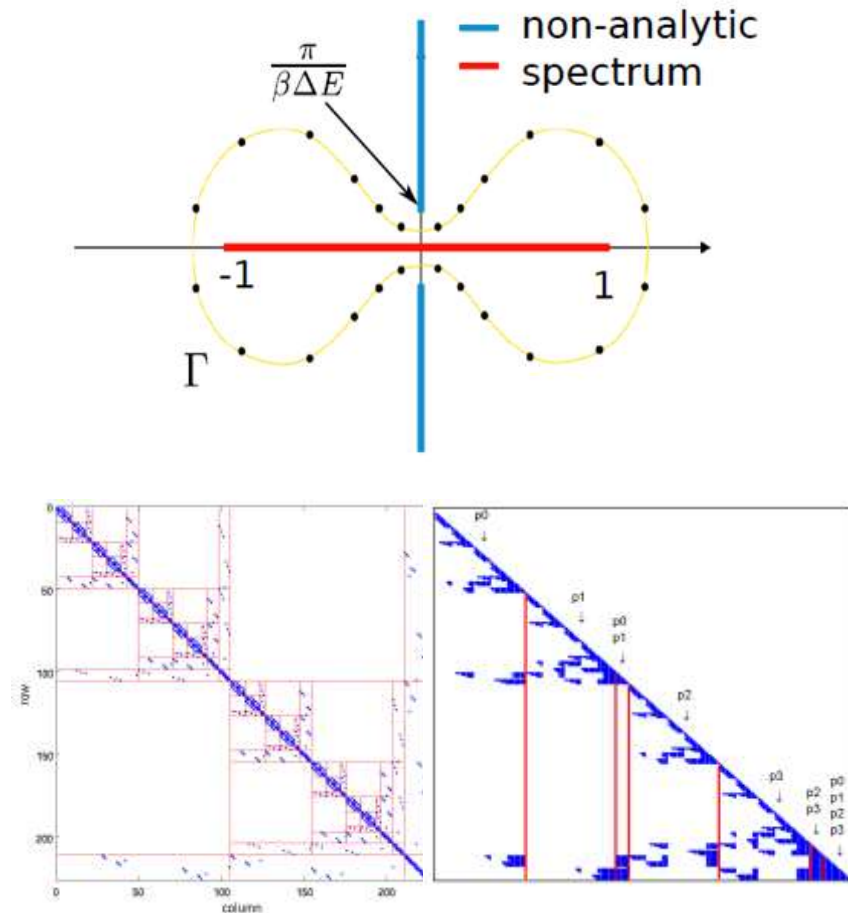
## X-ray absorption of liquid water : Summary

- ❑ Solve the XAS theoretical modeling in water
- ❑ Electron excitation theory is crucial to go beyond the DFT approach
- ❑ Self-consistent GW is important to obtain the correct transition matrix
- ❑ van der Waals interaction, correction of delocalization error by PBE0, nuclear quantum effect are all important
- ❑ Size of modeling the water is also important

# PEXSI (Pole Expansion and Selected Inversion)

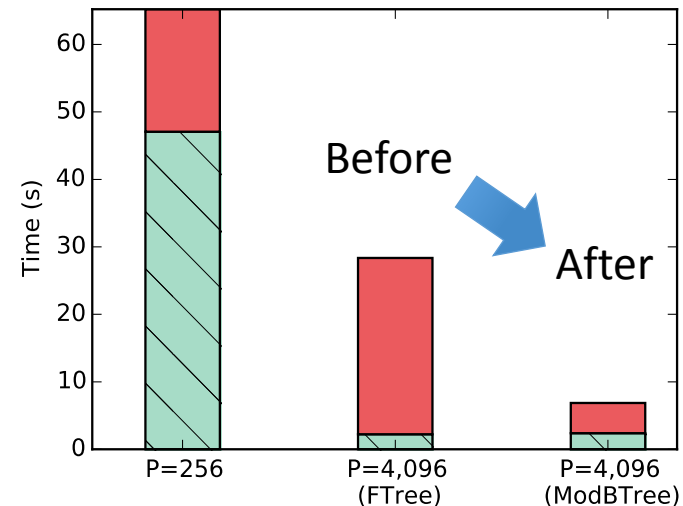
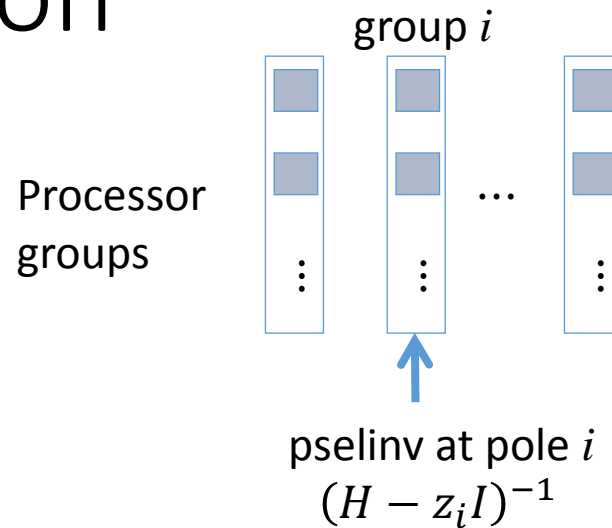
- An efficient way to evaluate electron density  $\rho = \text{diag}(XX^*)$ , energies and forces without diagonalizing Kohn-Sham Hamiltonian (L. Lin, R. Car, C. Yang, J. Lu, L. Ying, W. E) in ab initio MD simulation
- Pole expansion  

$$XX^* \approx \text{Im} \left[ \sum_i^M \omega_i (H - z_i I)^{-1} \right]$$
- Selected Inversion: compute selected entries of  $(H - z_i I)^{-1}$  using sparse matrix techniques.
- Complexity:  $O(n_e)$  for 1D,  $O(n_e^{3/2})$  for 2D,  $O(n_e^2)$  for 3D
- Work for both insulators and metals



# PEXSI Parallelization

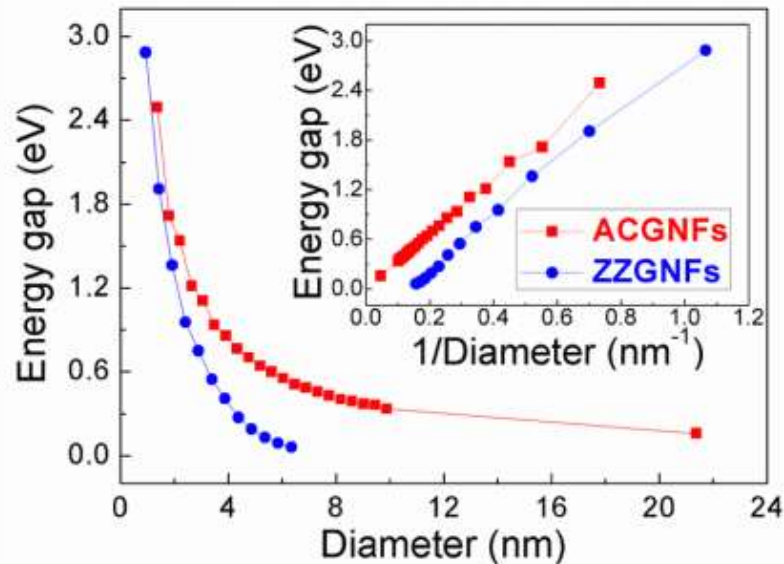
- Multi-level parallelism for high performance parallel computation
  - Embarrassing parallelization at the pole level.
  - Elimination tree level parallelism
  - Asynchronous communication
  - Overlap communication with computation
  - Tree-based restricted collective communication



[Jacquelin-Lin-Yang, ACM TOMS, 2015]

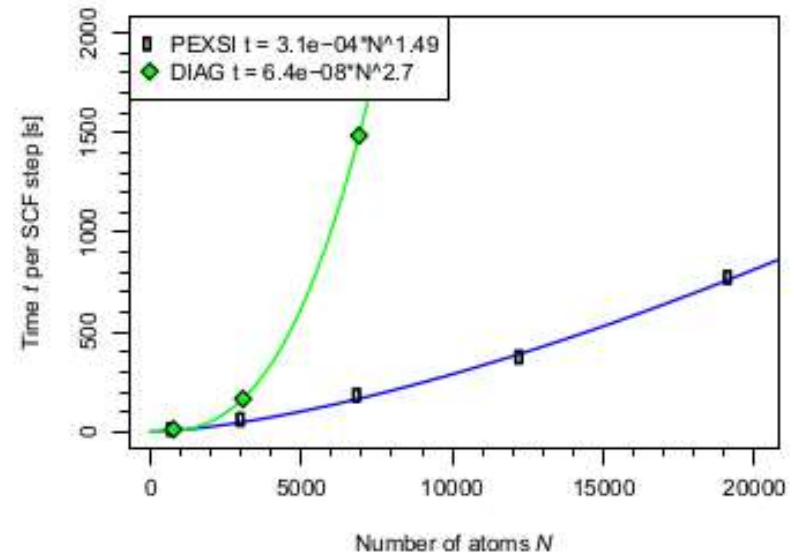
# Application

- Electronic structure of large-scale graphene nanoflakes of different edges.
- SIESTA-PEXSI for large system size: 11700 atoms



[Hu-Lin-Yang-Yang, JCP, 2014]

- Integrated with SIESTA, CP2K
- On-going SciDAC collaboration for electronic structure of WTe<sub>2</sub> layered systems.



Monolayer graphene

6400 cores used, 256 cores per pole, 50 poles

([http://manual.cp2k.org/trunk/CP2K\\_INPUT/FORCE\\_EVAL/DFT/LS\\_SCF/PEXSI.html](http://manual.cp2k.org/trunk/CP2K_INPUT/FORCE_EVAL/DFT/LS_SCF/PEXSI.html))



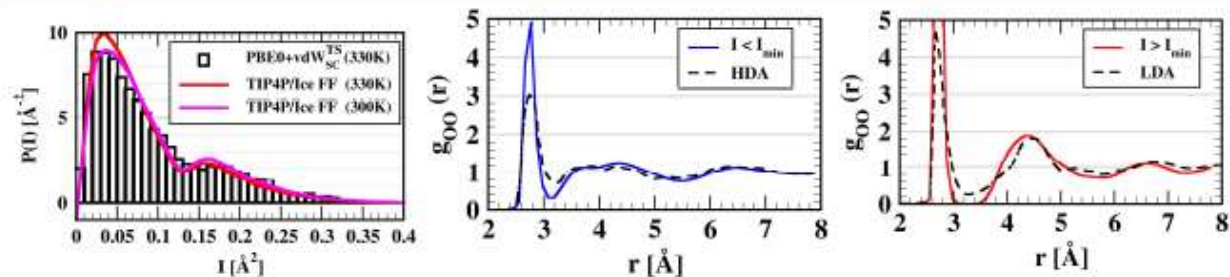


Figure 1 : Left panel:  $I$  distribution in the IPES from *ab initio* and model potentials. Middle panel:  $g_{00}(r)$  for low  $I$  sites compared to experimental  $g_{00}(r)$  of high density amorphous (HDA) ice. Right panel:  $g_{00}(r)$  for high  $I$  sites compared to the experimental  $g_{00}(r)$  of low density amorphous (LDA) ice.

3. Santra, B., DiStasio R. A. Jr., Martelli, F., and Car, R.. *Mol. Phys.*, [doi:10.1080/00268976.2015.1058432](https://doi.org/10.1080/00268976.2015.1058432)

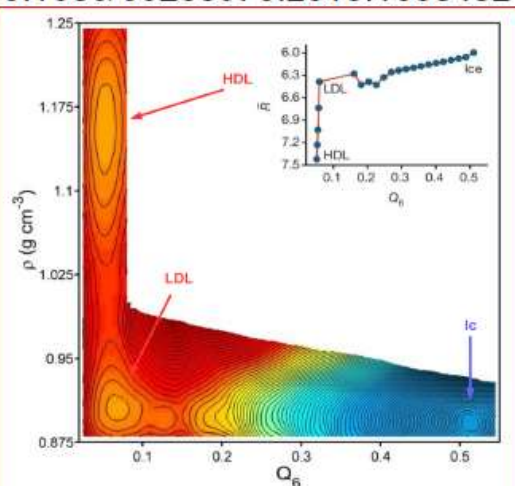


Figure 2 : Free energy plotted vs density and global order parameter  $Q_6$ . Simulations used 192 molecules at  $T = 228.6$  K and  $p = 2.2$  kbar.  $Q_6$  measures angular order. Inset: the average ring length  $\bar{R}$  as a function of  $Q_6$ .

- ▶ Monte Carlo simulations with enhanced sampling techniques show the existence of three basins in the free energy landscape of deeply supercooled ST2 water: a high density liquid (HDL) basin, a low density liquid (LDL) basin, and a stable cubic ice (Ic) basin<sup>4</sup>. The H-bond network shows a distinct topology, measured by the ring distribution, in each of these three basins.

4. Palmer, J. C., Martelli, F. Liu, Y. Car, R. Panagiotopoulos, A. Z. and Debenedetti, P. G., *Nature*, **510**, 385-388 (2014)

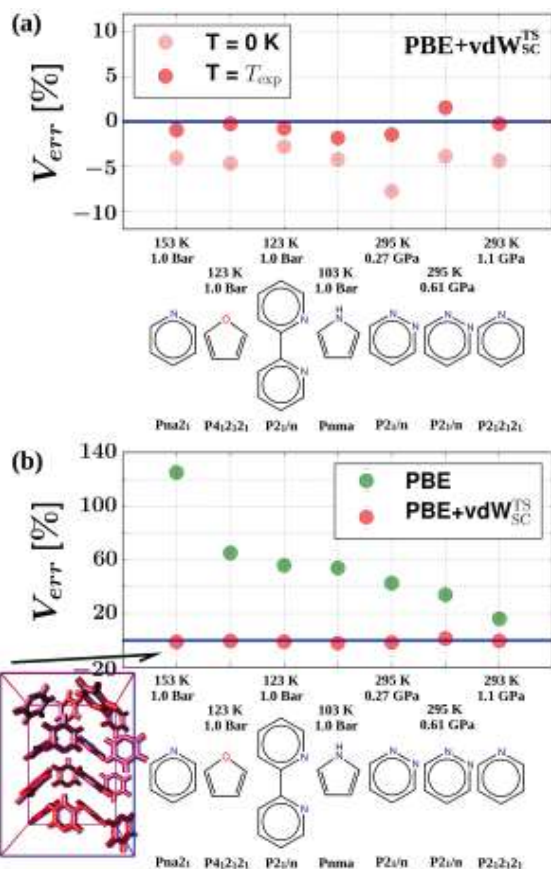


Figure 3: (a) PLMC structures from AIMD at  $p_{exp}$  and both  $T = 0$  K and  $T = T_{exp}$ . (b) PLMC structures from AIMD at  $p_{exp}$  and  $T_{exp}$  with and without vdW. The inset shows an overlay of the **calculated equilibrium structure** with the **experimental X-ray structure**.

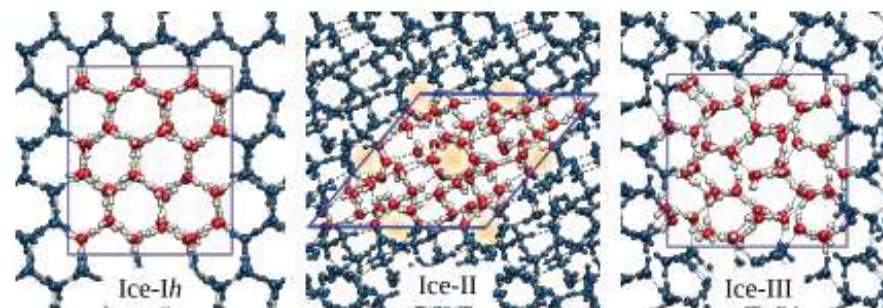


Figure 4: Snapshots of ice *Ih*, II, and III at the experimental triple point (0.21 GPa and 238 K).

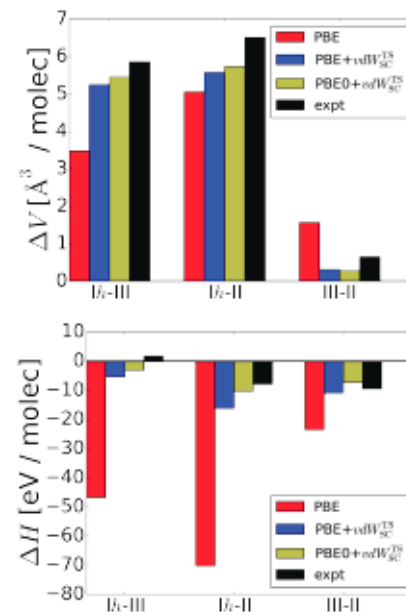


Figure 5: Volume ( $\Delta V$ ) and enthalpy ( $\Delta H$ ) differences between the ice phases at the triple point.

## The Phase Diagram of High-Pressure Superionic Ice

Jiming Sun,<sup>1</sup> Bryan K. Clark,<sup>2</sup> Salvatore Torquato,<sup>1,3,4</sup> and Roberto Car\*<sup>1,3,4</sup>

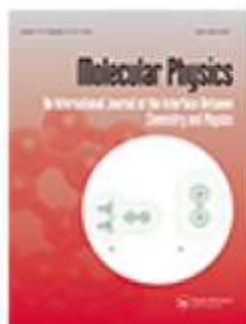
<sup>1</sup>*Department of Physics, Princeton University*

<sup>2</sup>*Department of Physics, University of Illinois at Urbana-Champaign*

<sup>3</sup>*Department of Chemistry, Princeton University*

<sup>4</sup>*Princeton Institute for the Science and Technology of Materials*

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#### A systematic study of chloride ion solvation in water using van der Waals inclusive hybrid density functional theory

Arindam Bankura<sup>a</sup>, Biswajit Santra<sup>b</sup>, Robert A. DiStasio Jr.<sup>b</sup>, Charles W. Swartz<sup>a</sup>, Michael L. Klein<sup>c</sup> & Xifan Wu<sup>c</sup>

<sup>a</sup> Institute for Computational Molecular Science and Department of Chemistry, Temple University, Philadelphia, PA, USA

<sup>b</sup> Department of Chemistry, Princeton University, Princeton, NJ, USA

<sup>c</sup> Department of Physics, Temple University, Philadelphia, PA, USA  
Published online: 06 Jul 2015.

- Nuclear quantum effects on important ions solutions
- Highly parallelized RPA-GW
- OH radical in water
- Thermodynamics of water
- Interfaces of water and functional materials

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